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# CP-Violating Effects in the Higgs Sector of the MSSM

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- ▶ Higgs sector in the MSSM with CP-phases
- ▶ Mass of the lightest Higgs boson
- ▶ Effective couplings

in coll. with M. Frank, T. Hahn, S. Heinemeyer, W. Hollik and G. Weiglein  
based on JHEP **0702** (2007) 047 [arXiv:hep-ph/0611326]

# Minimal Supersymmetric Standard Model (MSSM)

- ▶ supersymmetric extension of the standard model

## Supersymmetry (SUSY):

fermionic degrees of freedom  $\leftrightarrow$  bosonic degrees of freedom

$\Rightarrow$  superpartner for the standard model particles

- ▶ two Higgs doublets
- ▶ explicit SUSY breaking  $\Rightarrow$  many new (complex) parameters

# Complex Parameters

Complex parameters can lead to CP- or T-violation:

T-operator: **antiunitary**:

**complex conjugation** of complex parameters

MSSM: Parameters are complex in general:

They are not forbidden by a symmetry as

**CP-symmetry** is no fundamental symmetry in nature:

- ▶ observation of CP-violation in K- and B-systems
- ▶ CP-violation is needed for explanation of baryogenesis

# Two Higgs doublets

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Two reasons for two Higgs doublets:

- ▶ mass generation for both up- and down-type quarks

problem in contrast to SM:

charge conjugated Higgs superfield will break supersymmetry

- ▶ anomaly cancelations

problem in contrast to SM:

introduction of further fermions with non-vanishing hypercharges

# The Higgs potential in the MSSM

Higgs potential:

$$V_{\text{Higgs}} = \frac{g^2 + g'^2}{8} (H_1^+ H_1 - H_2^+ H_2)^2 + \frac{g^2}{2} |H_1^+ H_2|^2 + |\mu|^2 (H_1^+ H_1 + H_2^+ H_2) \\ + (m_1^2 H_1^+ H_1 + m_2^2 H_2^+ H_2) + (\epsilon_{ij} |m_{12}^2| e^{i\varphi} m_{12}^2 H_1^i H_2^j + h.c.)$$

$g, g'$ :

gauge couplings

$\mu$ :

coupl. betw. Higgs superfields

$m_1^2, m_2^2, m_{12}^2$ :

soft breaking parameters

one complex parameter:  $m_{12}^2 = |m_{12}^2| e^{i\varphi} m_{12}^2$

# The Higgs potential in the MSSM

if  $m_{12} = 0$  and  $\mu = 0$ :

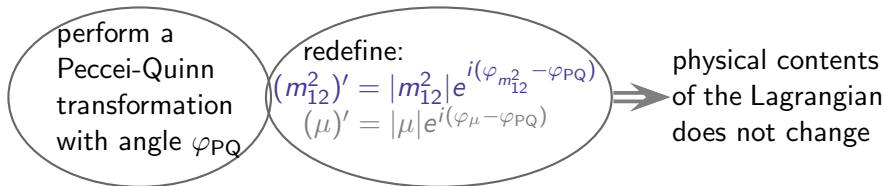
MSSM: further U(1) symmetry:  
Peccei-Quinn symmetry

# The Higgs potential in the MSSM

if  $m_{12} = 0$  and  $\mu = 0$ :

MSSM: further U(1) symmetry:  
Peccei-Quinn symmetry

if  $m_{12} \neq 0$  and  $\mu \neq 0$ :



$\Rightarrow$   $m_{12}^2$  can always be chosen to be real



# Higgs vacuum expectation values

Scalar Higgs doublets in the vacuum state:

$$H_1|_{\text{vac.}} = \begin{pmatrix} v_1 \\ 0 \end{pmatrix}, \quad H_2|_{\text{vac.}} = e^{i\xi} \begin{pmatrix} 0 \\ v_2 \end{pmatrix}$$



vacuum expectation values can differ by a phase  $\xi$

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vacuum expectation values can differ by a phase  $\xi$

Expansion about the vacuum:

$$H_1 = \begin{pmatrix} v_1 + \frac{1}{\sqrt{2}}(\phi_1^0 - i\zeta_1^0) \\ -\phi_1^- \end{pmatrix}, \quad H_2 = e^{i\xi} \begin{pmatrix} \phi_2^+ \\ v_2 + \frac{1}{\sqrt{2}}(\phi_2^0 + i\zeta_2^0) \end{pmatrix}$$

- four real scalar fields:  $\phi_1^0, \phi_2^0, \zeta_1^0, \zeta_2^0$
  - two complex scalar fields:  $\phi_1^\pm, \phi_2^\pm$
- } no mass eigenstates

# The Higgs sector at Born level

Mass terms: bilinear terms in the Higgs potential:

$$V_{\text{Higgs}}|_{\text{bil.}} = \frac{1}{2} (\phi_1^0, \phi_2^0) \mathcal{M}_{\phi^0} \begin{pmatrix} \phi_1^0 \\ \phi_2^0 \end{pmatrix} + \dots \text{ mixing betw. } (\phi_1^0, \phi_2^0), (\zeta_1^0, \zeta_2^0), \dots \\ + \frac{1}{2} (\phi_1^0, \phi_2^0) \mathcal{M}_{\phi^0\zeta^0} \begin{pmatrix} \zeta_1^0 \\ \zeta_2^0 \end{pmatrix} + \dots \text{ mixing betw. } (\phi_1^0, \phi_2^0, \zeta_1^0, \zeta_2^0)$$

Matrix  $\mathcal{M}_{\phi^0\zeta^0}$  generates mixing between the  $\phi^0$ - and  $\zeta^0$ -fields:

$$\mathcal{M}_{\phi^0\zeta^0} = \begin{pmatrix} 0 & m_{12}^2 \sin(\xi) \\ -m_{12}^2 \sin(\xi) & 0 \end{pmatrix}$$

$\implies$  no such mixing in case of real parameters

# The Higgs sector at Born level

Minimum condition for the vacuum:

$$\frac{\partial V_{\text{Higgs}}}{\partial H_j^i} \Big|_{\text{vac.}} = 0, \quad i, j = 1, 2$$

This is fulfilled if terms linear in the Higgs fields vanish:

$$V_{\text{Higgs}}|_{\text{lin}} = -t_{\phi_1^0} \phi_1^0 - t_{\phi_2^0} \phi_2^0 - t_{\zeta_1^0} \zeta_1^0 - t_{\zeta_2^0} \zeta_2^0$$

In particular:

$$t_{\zeta_1^0} = -\frac{v_1}{v_2} t_{\zeta_2^0} = \sqrt{2} m_{12}^2 v_2 \sin(\xi) \stackrel{!}{=} 0$$

⇒ phase  $\xi$  must **vanish**:  $\xi = 0$

at Born level: **no** CP-violating phases

# The Higgs sector at Born level

Physical mass eigenstates:

- ▶ 2 CP-even Higgs bosons:  $H^0, h^0$  ← mixing  $\phi_1^0, \phi_2^0$
- ▶ 1 CP-odd Higgs boson:  $A^0$  ← mixing  $\zeta_1^0, \zeta_2^0$
- ▶ 2 charged Higgs bosons:  $H^\pm$  ← mixing  $\phi_1^\pm, \phi_2^\pm$

Masses of the Higgs bosons:

- ▶ **not** all independent
- ▶ **lightest** Higgs boson:  $h^0$

upper theoretical Born mass limit:  $M_{h^0} \leq M_Z$

# The mass of the lightest Higgs boson

Real parameters:

upper theoretical Born mass limit:  $M_{h^0} \leq M_Z = 91 \text{ GeV}$

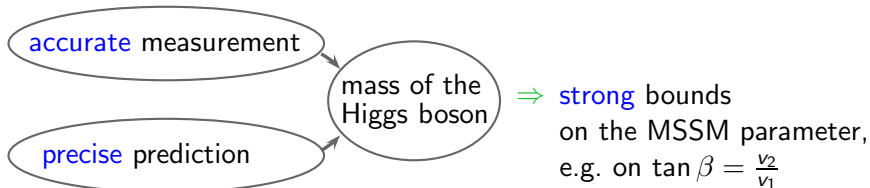
with quantum corrections of higher orders:  $M_{h^0} \lesssim 140 \text{ GeV}$

↪ dependent on the MSSM parameters

Complex parameters:

quantum corrections will also depend on parameter phases

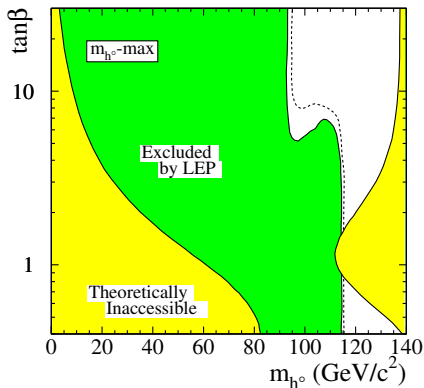
Discovery of the Higgs boson:



# The mass of the lightest Higgs boson

Before the discovery of the Higgs boson:

Exclusion of parts of the parameter space



Exclusion limits for  $\tan\beta$   
in the  $m_{h^0}\text{-max}$  scenario  
(real parameters)  
[LEP Higgs working group]

# Determination of the Higgs masses

Two-point-function:

$$-i\hat{\Gamma}(p^2) = p^2 - \mathbf{M}(p^2)$$

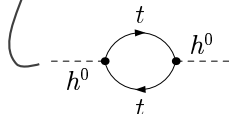
with the matrix:

$$\mathbf{M}(p^2) = \begin{pmatrix} M_{H^0}^2 - \hat{\Sigma}_{H^0 H^0}(p^2) & -\hat{\Sigma}_{H^0 h^0}(p^2) & -\hat{\Sigma}_{H^0 A^0}(p^2) \\ -\hat{\Sigma}_{H^0 h^0}(p^2) & M_{h^0}^2 - \hat{\Sigma}_{h^0 h^0}(p^2) & -\hat{\Sigma}_{h^0 A^0}(p^2) \\ -\hat{\Sigma}_{H^0 A^0}(p^2) & -\hat{\Sigma}_{h^0 A^0}(p^2) & M_{A^0}^2 - \hat{\Sigma}_{A^0 A^0}(p^2) \end{pmatrix}$$

Real parameters:

$$\hat{\Sigma}_{H^0 A^0}(p^2) = \hat{\Sigma}_{h^0 A^0}(p^2) = 0$$

no mixing between CP-even and CP-odd states





# Determination of the Higgs masses

- One way:

Propagator matrix:

$$\Delta(p^2) = -[\hat{\Gamma}(p^2)]^{-1}$$

Inversion of  $\hat{\Gamma} \Rightarrow$  diagonal propagators ( $i = H^0, h^0, A^0$ ):

$$\Delta_{ii}(p^2) = \frac{i}{p^2 - M_{i\text{Born}}^2 + \hat{\Sigma}_{ii}^{\text{eff}}(p^2)}$$

with the self energy term:

$$\hat{\Sigma}_{ii}^{\text{eff}}(p^2) = \hat{\Sigma}_{ii}(p^2) - i \frac{2\hat{\Gamma}_{ij}(p^2)\hat{\Gamma}_{jk}(p^2)\hat{\Gamma}_{ki}(p^2) - \hat{\Gamma}_{ki}^2(p^2)\hat{\Gamma}_{jj}(p^2) - \hat{\Gamma}_{ij}^2(p^2)\hat{\Gamma}_{kk}(p^2)}{\hat{\Gamma}_{jj}(p^2)\hat{\Gamma}_{kk}(p^2) - \hat{\Gamma}_{jk}^2(p^2)}$$

# Determination of the Higgs masses

Poles  $\mathcal{M}_i^2$  of the diag. propagators:

$$\mathcal{M}_i^2 - M_{i\text{Born}}^2 + \hat{\Sigma}_{ii}^{\text{eff}}(\mathcal{M}_i^2) = 0$$

Complex pole with phys. mass  $M$  and width  $\Gamma$  :

$$\mathcal{M}^2 = M^2 - iM\Gamma$$

Expansion around  $M^2$  up to first order in  $\Gamma$ :

$$M_i^2 - M_{i\text{Born}}^2 + \text{Re}\hat{\Sigma}_{ii}^{\text{eff}}(M_i^2) + \frac{\text{Im}\hat{\Sigma}_{ii}^{\text{eff}}(M_i^2) \left(\text{Im}\hat{\Sigma}_{ii}^{\text{eff}}\right)'(M_i^2)}{1 + \left(\text{Re}\hat{\Sigma}_{ii}^{\text{eff}}\right)'(M_i^2)} = 0$$

Iterative solution  $\Rightarrow$  Higgs masses  $M_i^2$

# Determination of the Higgs masses

- Second way:

Calculate the zeros of the determinant of  $\hat{\Gamma}$ :

$$\det[p^2 - \mathbf{M}(p^2)] = 0$$

or calculate the eigenvalues  $\lambda(p^2)$  of  $\mathbf{M}(p^2)$ :

$$\det[\lambda(p^2) - \mathbf{M}(p^2)] = 0$$

and solve iteratively:

$$p^2 - \lambda(p^2) = 0$$

# Higgs masses at higher orders (incl. CP-phases)

## Status:

- Higgs masses at higher order without CP-phases  $\Rightarrow$  good shape (up to leading 3-loop [Martin; Harlander, Kant, Mihaila, Steinhauser])

Including CP-phases:

- Eff. potential approach, up to two-loop leading-log contributions (sfermionic/fermionic contributions) [Pilaftsis, Wagner], [Demir], [Choi, Drees, Lee], [Carena, Ellis, Pilaftsis, Wagner]
- Gaugino contributions [Ibrahim, Nath]
- Effects of imaginary parts at one-loop [Ellis, Lee, Pilaftsis], [Choi, Kalinowski, Liao, Zerwas], [Bernabeu, Binosi, Papavassiliou]

**Here:** calculation in the Feynman diagrammatic approach

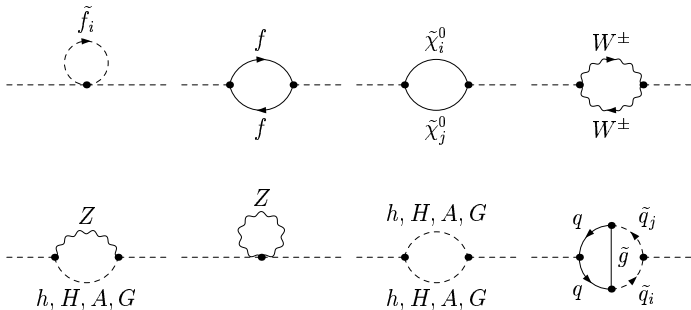
(full one-loop + two-loop  $\mathcal{O}(\alpha_t \alpha_s)$ )  $\alpha_t = \frac{\lambda_t^2}{4\pi}$ ,  $\lambda_t =$  Yukawa coupl.

# Renormalized self energies (SE)

Renormalized SE = Unrenormalized SE + Counterterm part

$$\hat{\Sigma} = \Sigma + \delta\Sigma$$

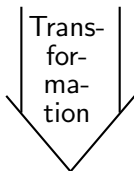
Feynman diagrams contributing to  $\Sigma$ :



# Parameters in the Higgs sector

Original parameters in the Higgs sector:

$g$     $g'$     $v_1$     $v_2$     $|m_{12}^2|$     $m_1^2$     $m_2^2$     $\xi$



$e$     $M_W$     $M_Z$     $\tan \beta$     $M_{H^\pm}$     $t_{h^0}$     $t_{H^0}$     $t_{A^0}$

electr.  
magn.  
coupl.  
const.

gauge  
boson  
masses

ratio  
of vac.  
exp. values  
 $\tan \beta = \frac{v_2}{v_1}$

mass  
of  
 $H^\pm$

tadpole  
parameter  
of  
 $h^0, H^0$

tadpole  
parameter  
of  
 $A^0$

# Mass matrix counterterm

Renormalization of the parameters:

$$M_x \rightarrow M_x + \delta M_x^{(1)} + \delta M_x^{(2)} + \dots \quad x = \{W, Z, H^\pm\}$$

$$\tan \beta \rightarrow \tan \beta + \delta \tan^{(1)} \beta + \delta \tan^{(2)} \beta + \dots$$

$$t_\phi \rightarrow t_\phi + \delta t_\phi^{(1)} + \delta t_\phi^{(2)} + \dots \quad \phi = \{H^0, h^0, A^0\}$$

Renormalization of the neutral Higgs mass matrix  $\mathcal{M}_n$ :

$$\mathcal{M}_n(M_x, \tan \beta, t_\phi) \rightarrow \mathcal{M}_n(M_x, \tan \beta, t_\phi)$$

$$+ \delta \mathcal{M}_n^{(1)}(M_x, \tan \beta, t_\phi, \delta M_x^{(1)}, \delta \tan^{(1)} \beta, \delta t_\phi^{(1)}) + \dots$$

# Higgs mass counterterms

$h^0$ -mass counterterm ( $\alpha =$  Born mixing angle of CP-even Higgses  $h^0, H^0$ ):

$$\begin{aligned}\delta M_{h^0}^{(1)} &= \cos^2(\alpha - \beta)(\delta M_{H^\pm}^2{}^{(1)} - \delta M_W^2{}^{(1)}) + \sin^2(\alpha + \beta)\delta M_Z^2{}^{(1)} \\ &+ \left[ (M_{H^\pm}^2 - M_W^2) \sin(2(\alpha - \beta)) + M_Z^2 \sin(2(\alpha + \beta)) \right] \cos^2 \beta \delta \tan^{(1)} \beta \\ &+ \frac{e \sin(\alpha - \beta)}{4M_W \sin \theta_W} \left[ (3 + \cos(2(\alpha - \beta))) \delta t_{h^0}^{(1)} + \sin(2(\alpha - \beta)) \delta t_{H^0}^{(1)} \right]\end{aligned}$$

“Mass” counterterm for the  $h^0$ - $A^0$ -mixing:

$$\delta M_{h^0 A^0}^{(1)} = \frac{e \sin(\alpha - \beta)}{2M_W \sin \theta_W} \delta t_{A^0}^{(1)}$$



# Renormalized Higgs self energies at one-loop

Renormalized  $h^0 h^0$ -self energy:

$$\hat{\Sigma}_{h^0 h^0}^{(1)}(p^2) = \Sigma_{h^0 h^0}^{(1)}(p^2) + \delta Z_{h^0 h^0}^{(1)}(p^2 - M_{h_{\text{Born}}^0}^2) - \delta M_{h^0}^{(1)}$$

with the field renormalization constant:

$$\delta Z_{h^0 h^0}^{(1)} = \sin^2 \alpha \delta Z_{H_1}^{(1)} + \cos^2 \alpha \delta Z_{H_2}^{(1)}$$

Field renormalization of the Higgs doublets:

$$H_i \rightarrow \left( \mathbb{1} + \frac{1}{2} \delta Z_{H_i}^{(1)} + \dots \right) H_i \quad i = 1, 2$$

Renormalized  $h^0 A^0$ -mixing:

$$\hat{\Sigma}_{h^0 A^0}^{(1)}(p^2) = \Sigma_{h^0 A^0}^{(1)}(p^2) - \delta M_{h^0 A^0}^{(1)}$$

# Renormalization conditions

Within an  $\overline{\text{DR}}$ /on-shell scheme in the Higgs sector:

- ▶ define the  $H^{\pm}$ -,  $W$ - as well as the  $Z$ -mass as **pole mass**  
⇒ directly related to a **physical observable**

$$\delta M_X^{(1)} = \text{Re} \Sigma_{XX}^{(1)}(M_X^2), \quad X = \{H^{\pm}, W, Z\}$$

- ▶ **no** shift of the minimum of the Higgs potential

$$\delta t_{\phi}^{(1)} = -T_{\phi}^{(1)}$$

- ▶  $\overline{\text{DR}}$ -scheme for field and  $\tan \beta$  renormalization

$$\delta \tan^{(1)} \beta = \delta \tan \beta^{\overline{\text{DR}}}, \quad \delta Z_{H_i}^{(1)} = \delta Z_{H_i}^{\overline{\text{DR}}}$$

# Phases in other sectors

- Sfermion sector:

- ▶ phase  $\varphi_{A_f}$  of the trilinear coupling  $A_f$

- Higgsino sector:

- ▶ phase of  $\mu$

- Gaugino sector:

- ▶ phases of the gaugino mass parameters  $M_1, M_2, M_3$

- one phase can be eliminated (R-Transformation), often  $\varphi_{M_2}$

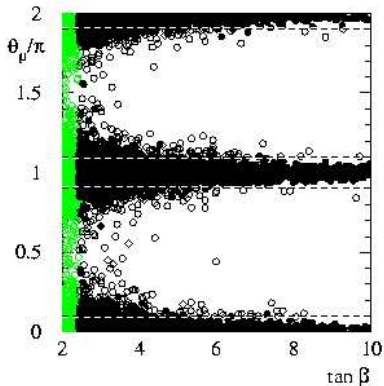
- phase  $\varphi_{M_3}$  is the phase of the gluino mass parameter

- ⇒ enters into the Higgs sector at two-loop level

soft breaking  
parameter

# Phase of $\mu$

Constrained by measurements of electric dipole moments:



15 parameter scan:

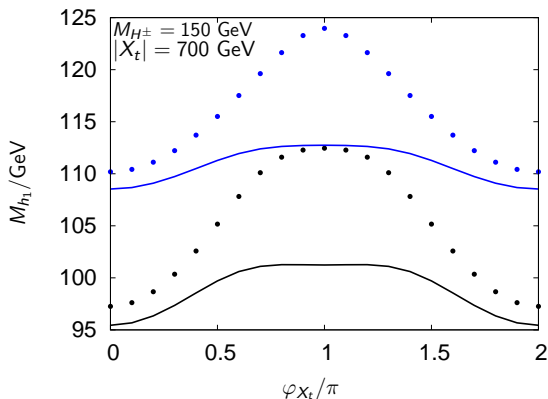
allowed values: black dots

[Barger, Falk, Han, Jiang,  
Li, Plehn]

- In large areas: The phase of  $\mu$  is small.

# Results: $\varphi_{X_t}$ -dependence

Size of the squark mixing:  $X_t := A_t - \mu^* \cot \beta$

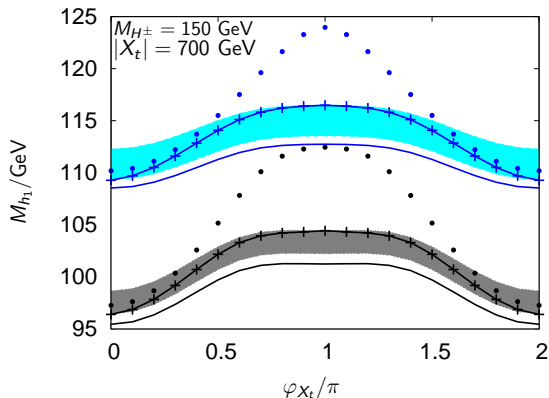


- Higgs mass  $M_{h_1}$  does depend on the phase  $\varphi_{X_t}$ ,  $|X_t| = 700$  GeV.

$\mathcal{O}(\alpha)$ :  $\tan \beta = 5$    •   •    $\tan \beta = 15$   
 $\mathcal{O}(\alpha + \alpha_t \alpha_s)$ :  $\tan \beta = 5$    —   —    $\tan \beta = 15$

# Results: $\varphi_{X_t}$ -dependence

Size of the squark mixing:  $X_t := A_t - \mu^* \cot \beta$



**Bands:** Estimate of the size of the corrections of  $\mathcal{O}(\alpha_b \alpha_s + \alpha_t^2 + \alpha_t \alpha_b + \alpha_b^2)$  [Slavich et al.], FeynHiggs

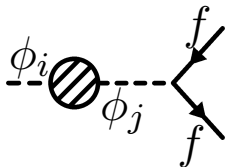
**Interpolation:** Size of above corrections known for the MSSM with **real** parameters: Evaluate for  $\varphi_{X_t} = 0$  and  $\varphi_{X_t} = \pi$  and interpolate

$\mathcal{O}(\alpha) : \tan \beta = 5$     •    •     $\tan \beta = 15$   
 $\mathcal{O}(\alpha + \alpha_t \alpha_s) : \tan \beta = 5$     —    —     $\tan \beta = 15$   
 $\mathcal{O}(\alpha + \alpha_t \alpha_s) + \text{interpol.} : \tan \beta = 5$     —+—+—     $\tan \beta = 15$

# Amplitudes with external Higgs bosons

**Mixing** between the Higgs bosons:

( $\overline{\text{DR}}$ /on-shell scheme)  $\phi_{\{i,j\}} = H^0, h^0, A^0$



Finite wave function normalization factors needed:

$$\sqrt{\hat{Z}_i(\Gamma_i + \hat{Z}_{ij}\Gamma_j + \hat{Z}_{ik}\Gamma_k)}$$

$\hat{Z}_i$  ensures that the residue is set to 1:

$$\hat{Z}_i = \frac{1}{1 + \left(\text{Re}\hat{\Sigma}_{ii}^{\text{eff}}\right)'(M_i^2)}$$

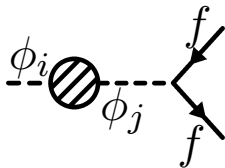
$\hat{Z}_{ij}$  describes transition  $i \rightarrow j$ :

$$\hat{Z}_{ij} = \frac{\Delta_{ij}(p^2)}{\Delta_{ii}(p^2)} \Big|_{p^2=M_i^2}$$

# Amplitudes with external Higgs bosons

**Mixing** between the Higgs bosons:

( $\overline{\text{DR}}$ /on-shell scheme)  $\phi_{\{i,j\}} = H^0, h^0, A^0$



Finite wave function normalization factors needed:

$$\sqrt{\hat{Z}_i(\Gamma_i + \hat{Z}_{ij}\Gamma_j + \hat{Z}_{ik}\Gamma_k)}$$

Mixing matrix ( $\hat{Z}_{ii} = 1$ ):

$$\tilde{Z}_{ij} = \sqrt{\hat{Z}_i\hat{Z}_{ij}}$$

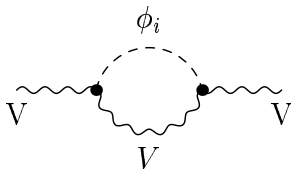
Vertex with external Higgs boson:

$$\tilde{Z}_{ii}\Gamma_i + \tilde{Z}_{ij}\Gamma_j + \tilde{Z}_{ik}\Gamma_k$$



# Amplitudes with internal Higgs bosons

Diagrams with internal Higgs bosons enter precision observables (W-mass, ...):



- Calculation with Born states  $\phi_i = H^0, h^0, A^0$ : no problem
- Calculation with  $\phi_i = h_1, h_2, h_3 \Rightarrow$  Inclusion of higher order effects:

One possibility: Use of effective couplings:

Consider  $\tilde{\mathbf{Z}}_{ij}$  as mixing matrix:

Problem:  $\tilde{\mathbf{Z}}_{ij}$  is a non-unitary matrix  
(no rotation matrix)

$\Rightarrow$  further approximations necessary

# Amplitudes with internal Higgs bosons

Further approximations ( $\hat{=}$  effective potential approach):

$$\tilde{\mathbf{Z}}(\hat{\Sigma}(p^2)) \rightarrow \tilde{\mathbf{Z}}(\hat{\Sigma}(0)) = \mathcal{R}$$

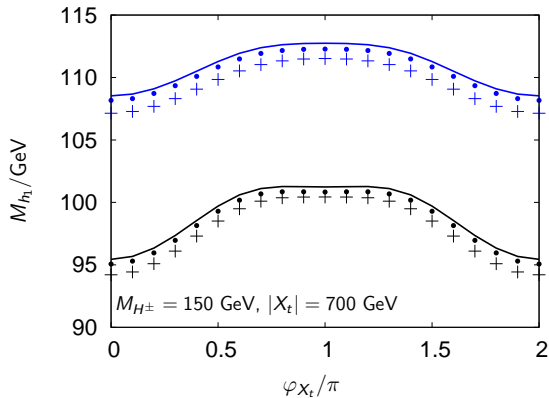
$\mathcal{R}$  diagonalizes matrix  $\mathbf{M}(0)$ :

$$\begin{pmatrix} h_1 \\ h_2 \\ h_3 \end{pmatrix}_{p^2=0} = \mathcal{R} \begin{pmatrix} H^0 \\ h^0 \\ A^0 \end{pmatrix}, \quad \mathcal{R} \mathbf{M}(0) \mathcal{R}^\dagger = \begin{pmatrix} M_{h_1, p^2=0}^2 & 0 & 0 \\ 0 & M_{h_2, p^2=0}^2 & 0 \\ 0 & 0 & M_{h_3, p^2=0}^2 \end{pmatrix}$$

Other possibility: use  $\mathcal{U}$ :  $\hat{\Sigma}_{ii}(p_{\text{OS}}^2 = M_{i\text{Born}}^2)$ ,  $\hat{\Sigma}_{ij}(p_{\text{OS}}^2 = (M_{i\text{Born}}^2 + M_{j\text{Born}}^2)/2)$ :

$$\begin{pmatrix} h_1 \\ h_2 \\ h_3 \end{pmatrix}_{p_{\text{OS}}^2} = \mathcal{U} \begin{pmatrix} H^0 \\ h^0 \\ A^0 \end{pmatrix}, \quad \mathcal{U} \text{Re}(\mathbf{M}(p_{\text{OS}}^2)) \mathcal{U}^\dagger = \begin{pmatrix} M_{h_1, p_{\text{OS}}^2}^2 & 0 & 0 \\ 0 & M_{h_2, p_{\text{OS}}^2}^2 & 0 \\ 0 & 0 & M_{h_3, p_{\text{OS}}^2}^2 \end{pmatrix}$$

# Results: $\varphi_{X_t}$ -dependence of $M_{h_1}$ (diff. approx.)



no approx.: $\tan \beta = 5$	—	$\tan \beta = 15$
$p_{\text{OS}}^2$ -approx.: $\tan \beta = 5$	•	$\tan \beta = 15$
$p^2 = 0$ -approx.: $\tan \beta = 5$	+	$\tan \beta = 15$


- The different approximations apply only for the **one-loop** contributions (two-loop contr. are calculated with  $p^2 = 0$ ).
- The  $p^2 = 0$ -result differs by up to 1.5 GeV from the full result.
- The  $p_{\text{OS}}^2$ -result differs by less than 0.5 GeV from the full result.

# Couplings

One example:

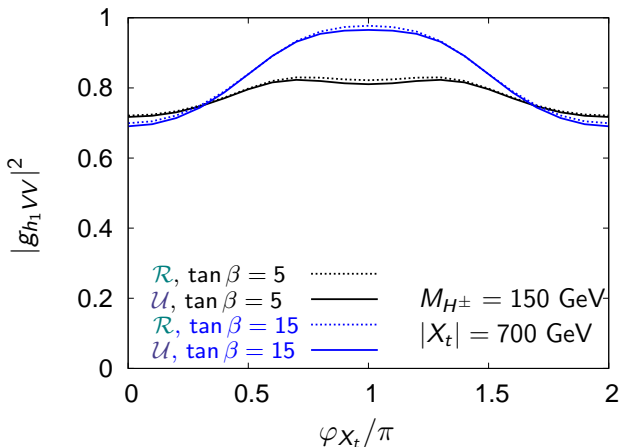
Coupling of two gauge bosons ( $V = W, Z$ ) and one Higgs boson:

$$g_{h_i VV} = [U_{i1} \cos(\beta - \alpha) + U_{i2} \sin(\beta - \alpha)] g_{H_{SM} VV}$$

standard model coupling 

- only CP-even components of the Higgs bosons couple to  $V$
- all three Higgs bosons can have a CP-even component

# Results: $\varphi_{X_t}$ -dependence of couplings



- Here:  $g_{h_1 VV}$  is normalized to the standard model coupling.
- $|g_{h_1 VV}|^2$  does depend on the phase  $\varphi_{X_t}$ .
- $\mathcal{R}_{p^2=0}$  and  $\mathcal{U}_{pOS}$  give similar results with only tiny differences.

# Summary

- ▶ At **Born** level: **no** CP-violation in the Higgs sector
- ▶ **Quantum corrections** can **induce** CP-violation.
- ▶ **Quantum corrections** have to be taken into account:
  - prediction of Higgs boson masses
  - amplitudes with external Higgs bosons  $\Rightarrow \tilde{Z}$
  - amplitudes with internal Higgs bosons  $\Rightarrow \mathcal{R}, \mathcal{U}$
- ▶ The **full one-loop** and the **two-loop**  $\mathcal{O}(\alpha_t \alpha_s)$  contributions with the **complete phase dependence** are implemented into FeynHiggs.
- ▶ **FeynHiggs2.6** is available at [www.feynhiggs.de](http://www.feynhiggs.de) .