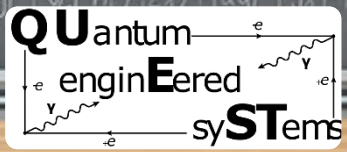
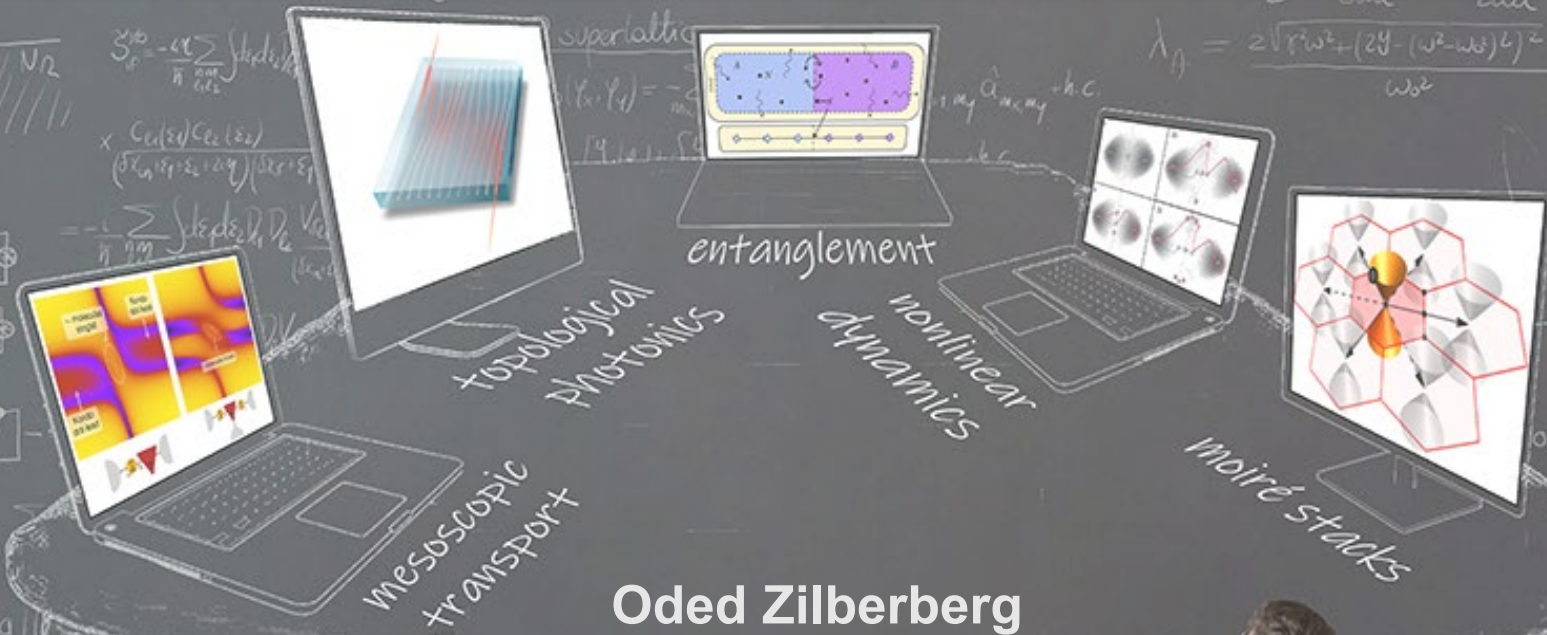


Electronic, atomic, and photonic QUantum Engineered SysTems



Eidgenössische Technische Hochschule Zürich
Swiss Federal Institute of Technology Zürich



SWISS NATIONAL SCIENCE FOUNDATION

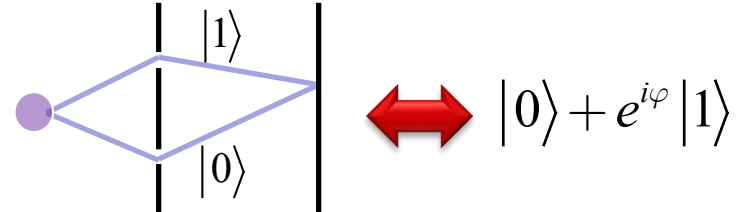


Quantum mechanical journey

Discovery (1920s)
Particle-wave duality



Superposition and coherence



Quantum mechanical journey

Discovery (1920s)
Particle-wave duality



Superposition and coherence

● $|0\rangle + e^{i\varphi} |1\rangle$

Philosophy (1935-1990)
EPR paradox



Entanglement

● ● $(|0\rangle + |1\rangle) \otimes (|0\rangle + |1\rangle)$
 $|00\rangle + |01\rangle + |10\rangle + |11\rangle$
 $|00\rangle + |~~10~~\rangle + |~~01~~\rangle + |11\rangle$

Quantum mechanical journey

Discovery (1920s)
Particle-wave duality



Superposition and coherence

● $|0\rangle + e^{i\varphi} |1\rangle$

Philosophy (1935-1990)
EPR paradox



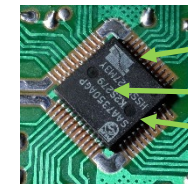
Entanglement

● ● $|00\rangle + |11\rangle$

Material engineering (1930s-today)
Applications



Integrated circuits



Conductors

Semiconductors

Insulators

Quantum mechanical journey

Discovery (1920s)
Particle-wave duality



Superposition and coherence



$$|0\rangle + e^{i\varphi} |1\rangle$$

Philosophy (1935-1990)
EPR paradox



Entanglement

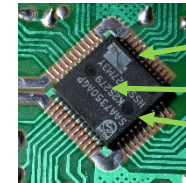


$$|00\rangle + |11\rangle$$

Material engineering (1930s-today)
Applications



Integrated circuits



Conductors

Semiconductors

Insulators

Quantum engineering (1980s-today)
Future technology

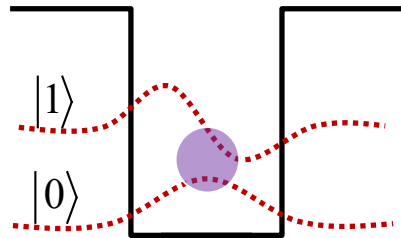


Control, manipulate,
 and harness
quantum resources

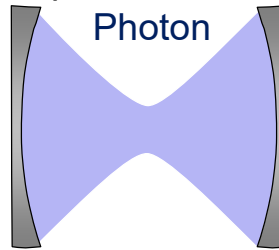
Control, manipulate, and harness

Superposition and coherence

Trap quantum particles

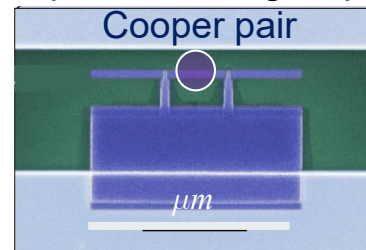


Optical cavities



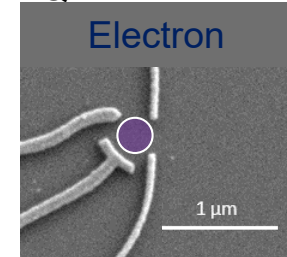
RMP **85**, 1083 (2013)

Superconducting loops



Nature **431**, 162 (2004)

Quantum dots

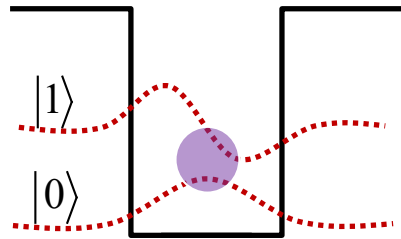


PRL **115**, 166603 (2015)

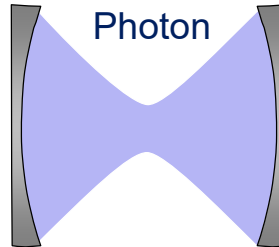
Control, manipulate, and harness

Superposition and coherence

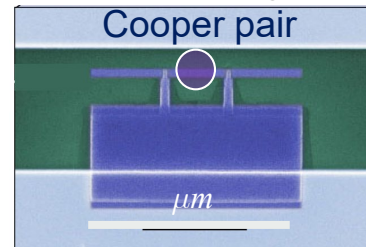
Trap quantum particles



Optical cavities

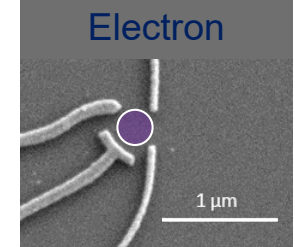


Superconducting loops



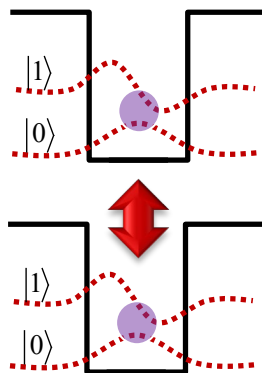
Nature **431**, 162 (2004)

Quantum dots

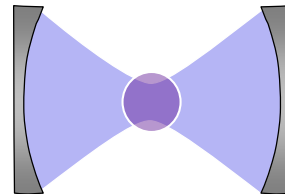


PRL **115**, 166603 (2015)

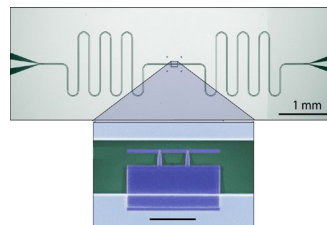
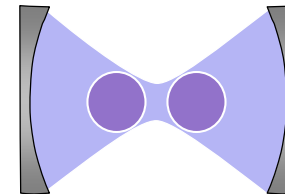
Entanglement



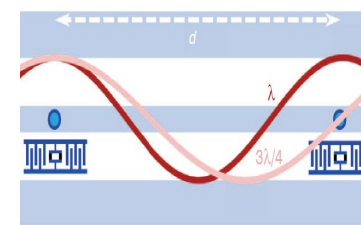
atom-photon



atom-atom



Nature **431**, 162 (2004)



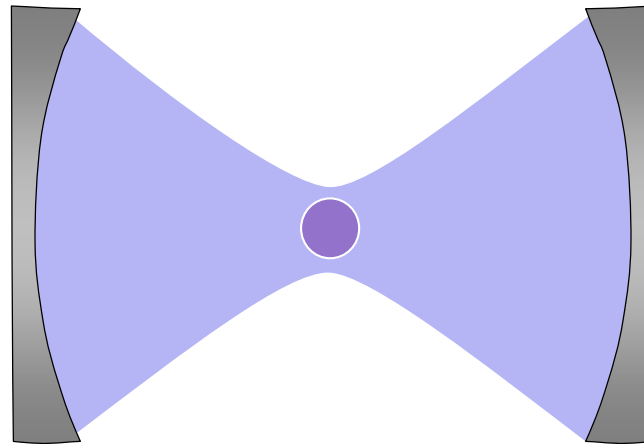
Science **342**, 1494 (2013)

QUEST research

Coherence



Open system



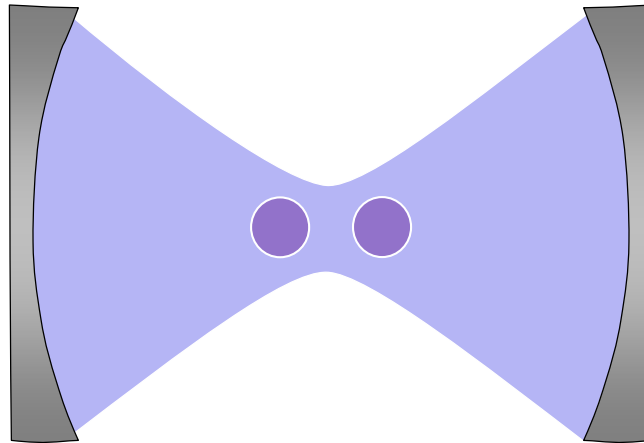
1

QUEST research

Coherence



Open system



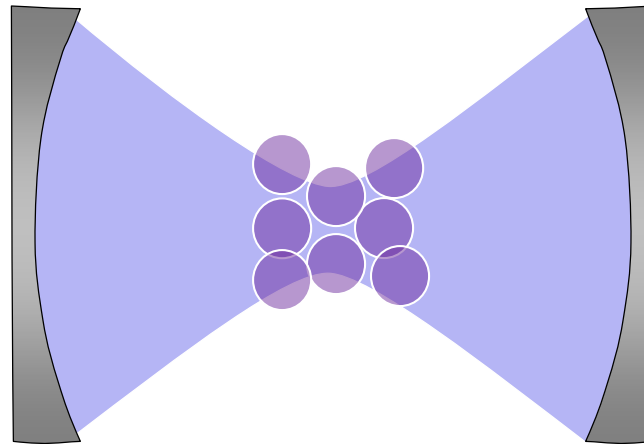
2

QUEST research

Coherence



Open system



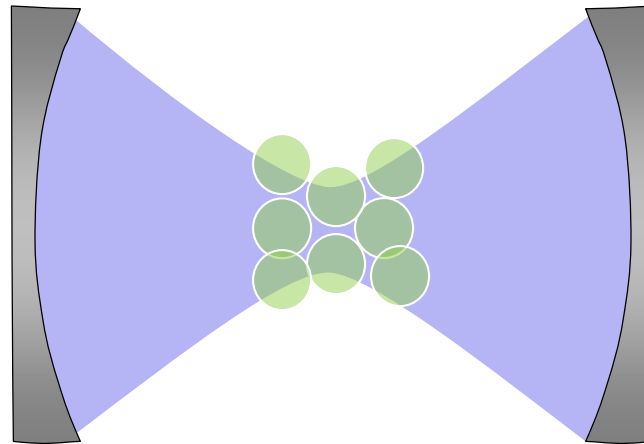
many

QUEST research

Coherence



Open system



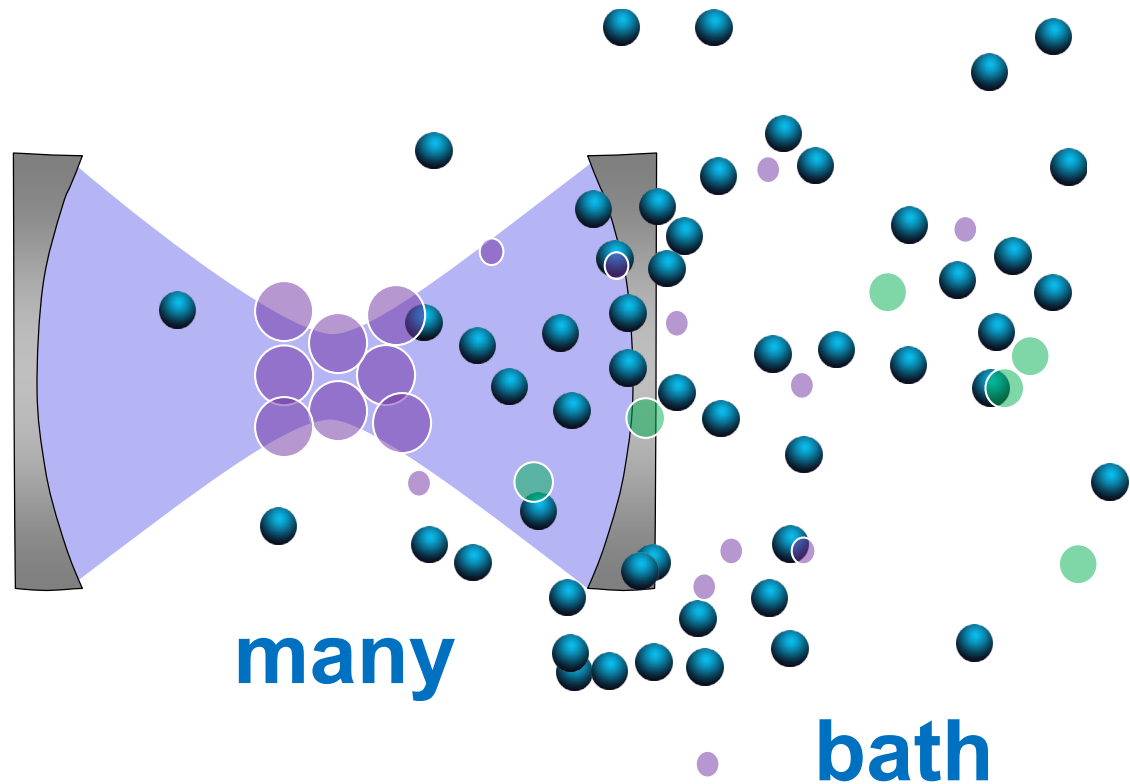
bosons ↔ fermions

QUEST research

Coherence



Open system

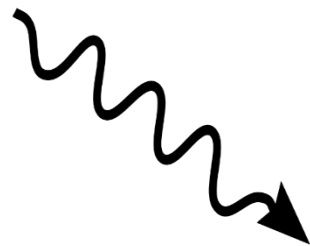


QUEST research

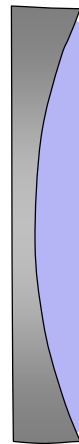
Coherence



Open system

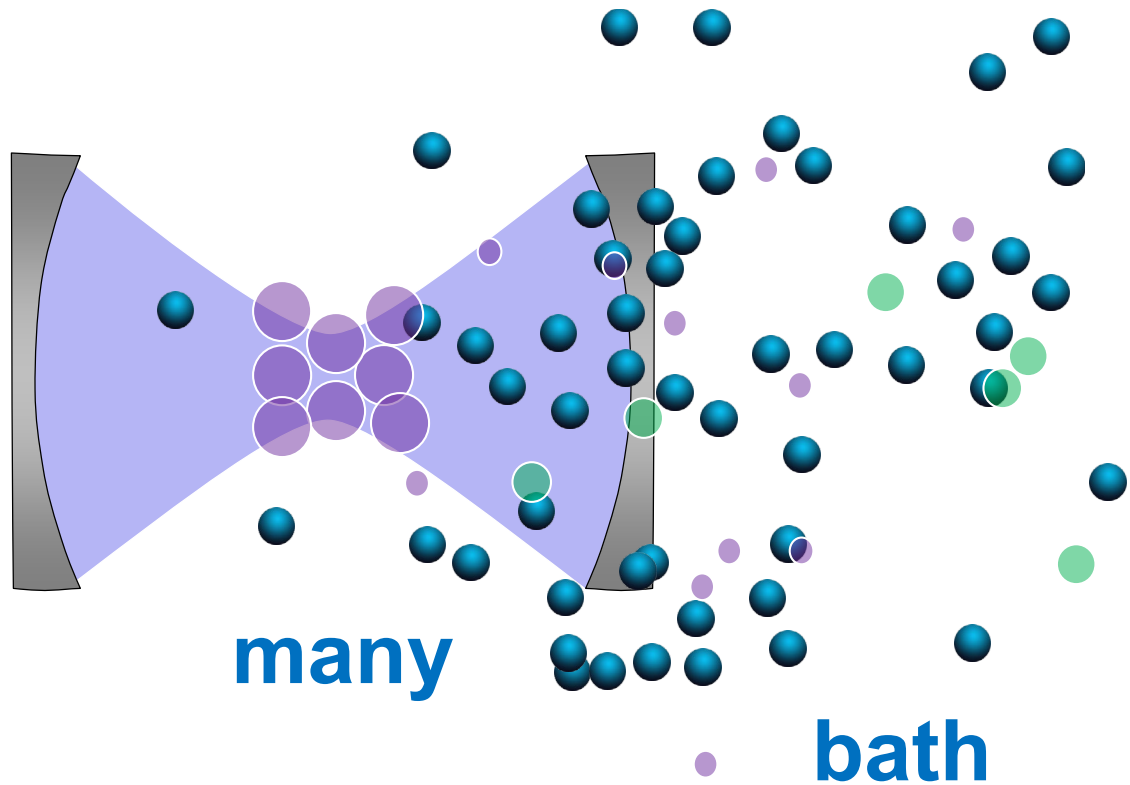


drive



many

bath



Quantum simulation

Cold atoms

$\sim 1\mu\text{m}$
 $\sim 1\text{nK}$
 $\sim 10^{-10}\text{meV}$

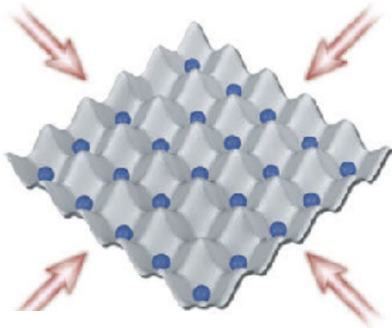
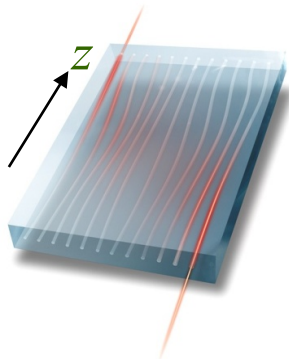


Figure from Bloch, Nature 453, 1016 (2008)

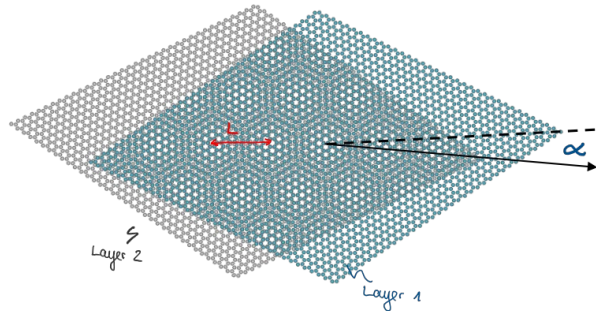


Photons

$\sim 1\mu\text{m}$
 $\sim 5/\text{cm}$

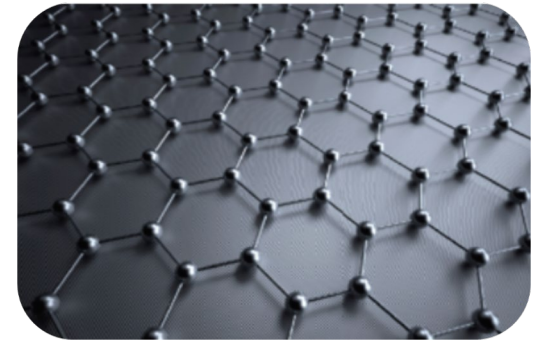
Moiré lattices

$\sim 10\text{nm}$
 $\sim 1\text{K}$
 $\sim 0.1\text{meV}$



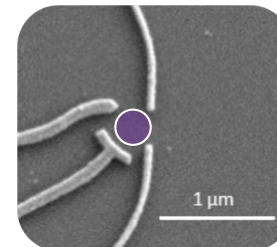
Condensed matter

$\sim \text{few } \text{\AA}$
 $100\text{-}1000\text{K}$
 $\sim 10\text{-}100\text{meV}$



Mesoscopic devices

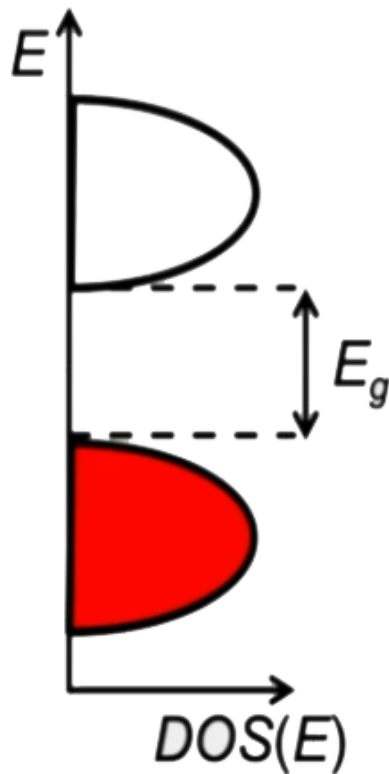
$\sim 10\text{-}1000\text{nm}$
 $\sim 10\text{mK}$
 $\sim 10\text{-}100\text{meV}$



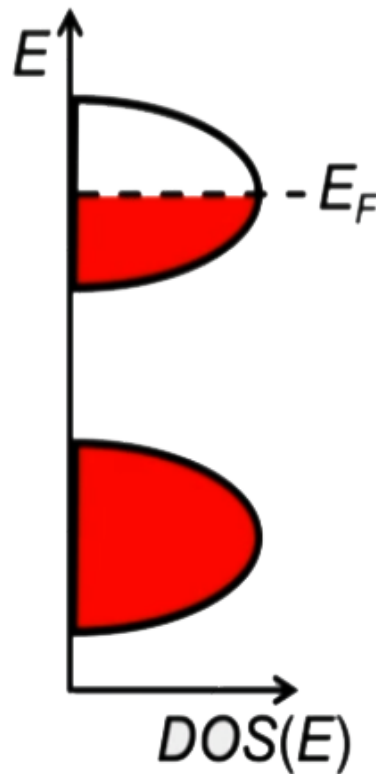
From single to many-body physics

Single-particle Band Theory

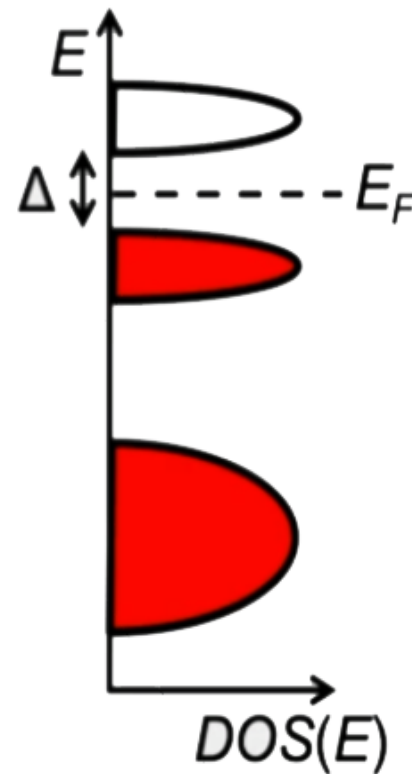
Insulator



Metal



Correlated Insulator

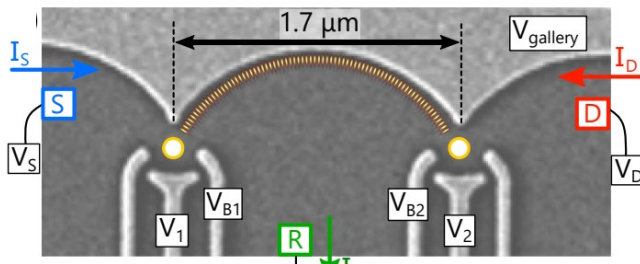


QUEST research

Quantum engineering of

Devices

Mesoscopic transport



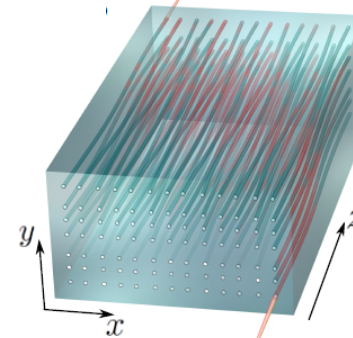
engineered quantum chemistry



many-body cond. mat.

Material properties

Quantum simulation



designer models



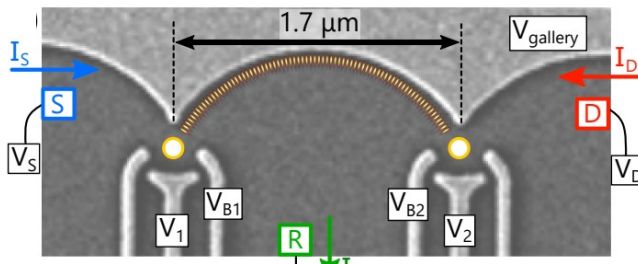
real materials

QUEST research

Quantum engineering of

Devices

Mesoscopic transport



engineered quantum chemistry

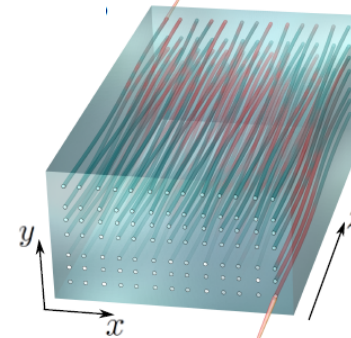


many-body cond. mat.

- Electronic interferometers
- Kondo impurities
- Quantum measurement
- Topological semimetals

Material properties

Quantum simulation



designer models



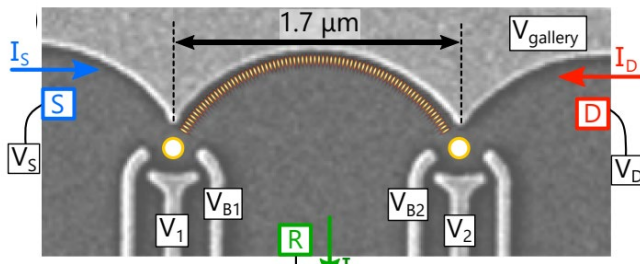
real materials

QUEST research

Quantum engineering of

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Mesoscopic transport



engineered quantum chemistry

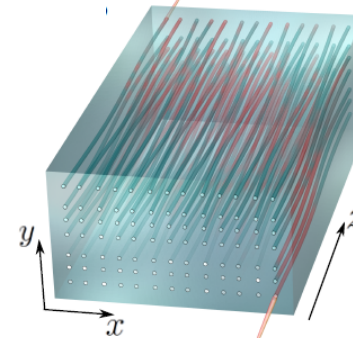


many-body cond. mat.

- Electronic interferometers
- Kondo impurities ←
- Quantum measurement
- Topological semimetals

Material properties

Quantum simulation



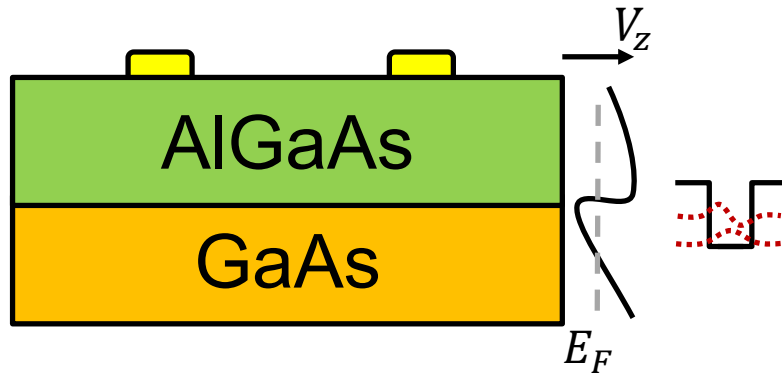
designer models



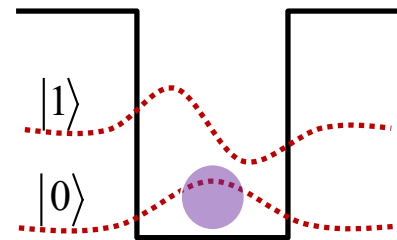
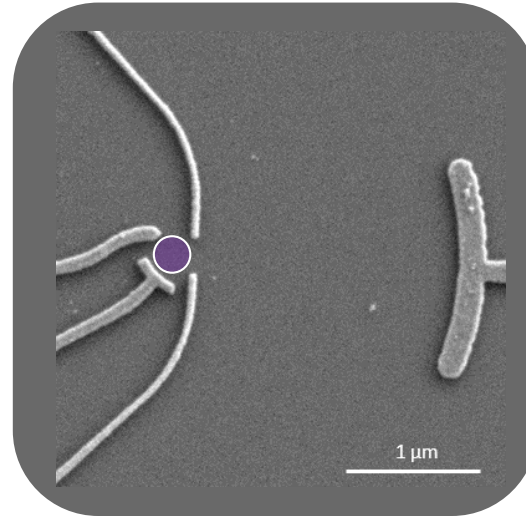
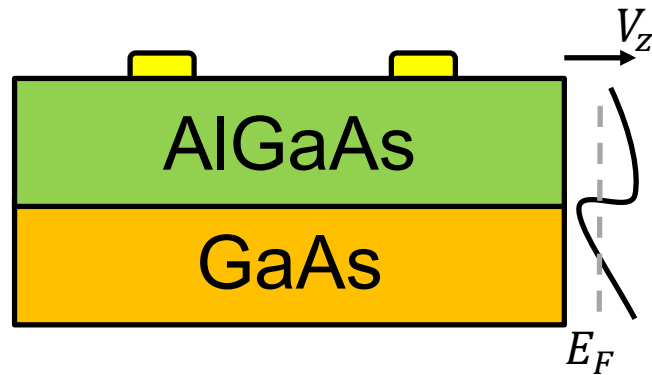
real materials

- Topological photonics
- Synthetic dimensions
- Quasicrystals
- Dissipative phase transitions

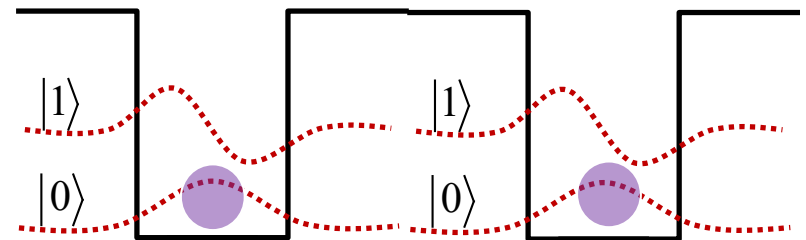
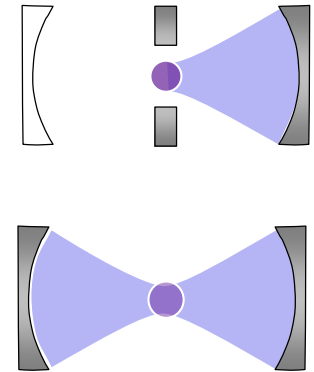
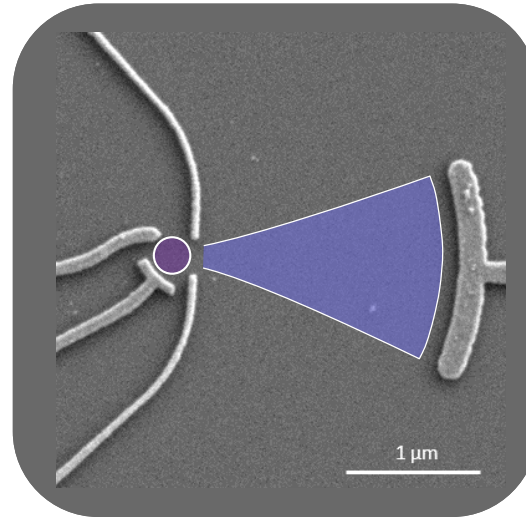
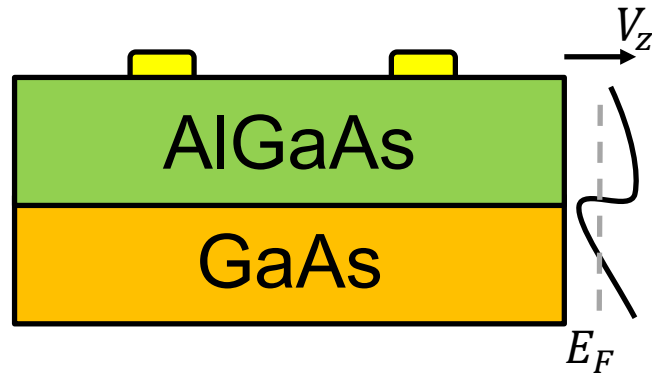
Material progress \Rightarrow engineer electron landscape



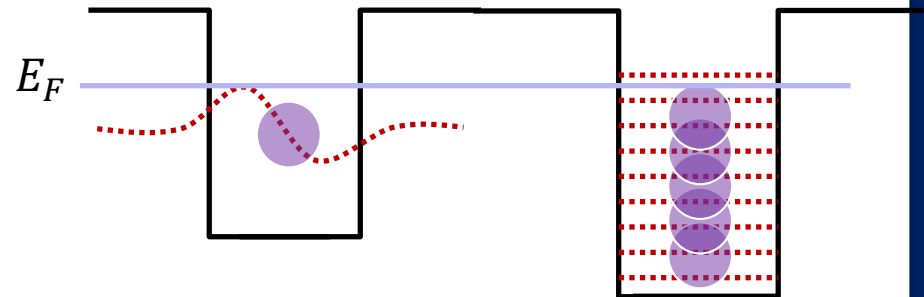
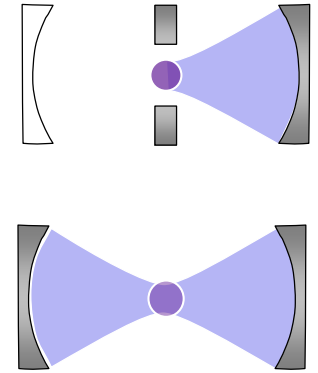
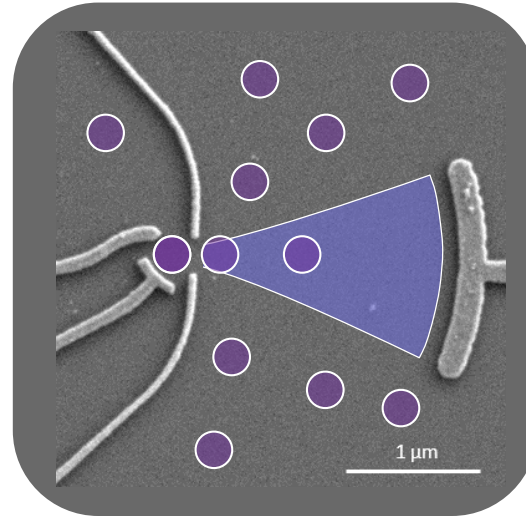
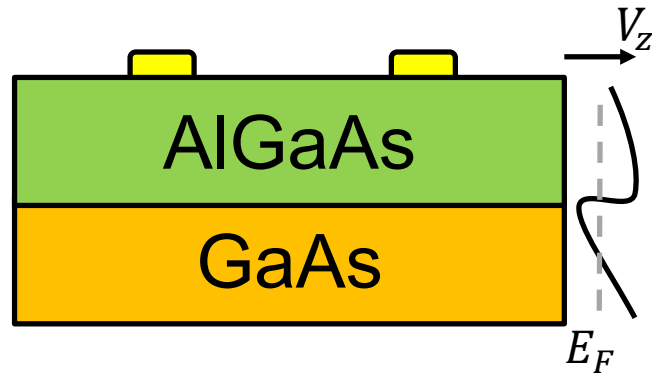
Material progress \Rightarrow engineer electron landscape



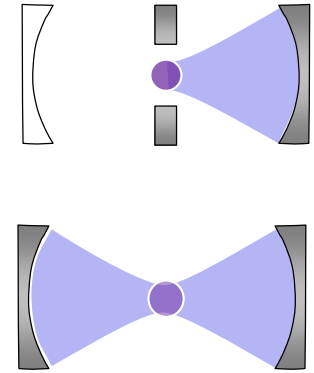
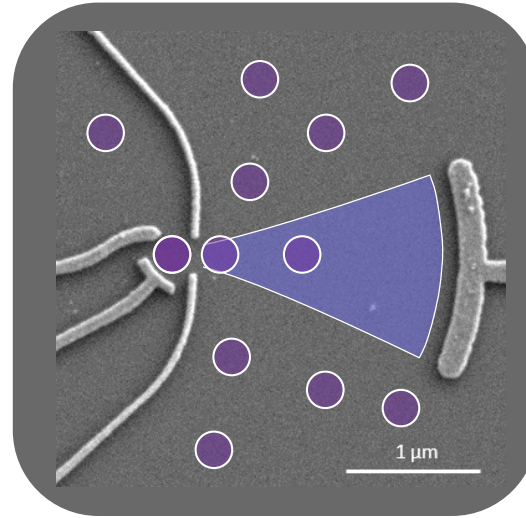
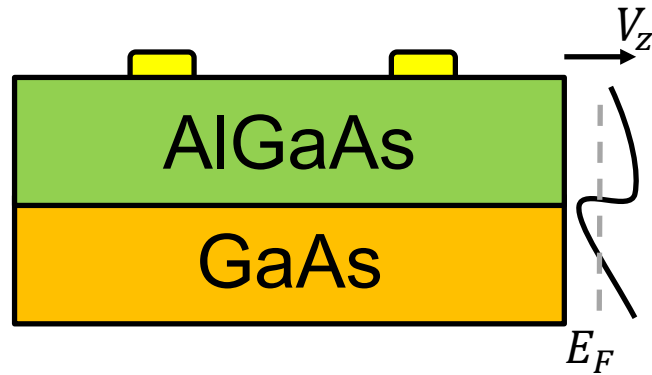
Material progress \Rightarrow engineer electron landscape



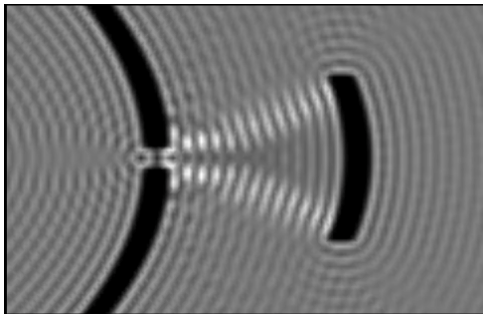
Many-body Fermi sea



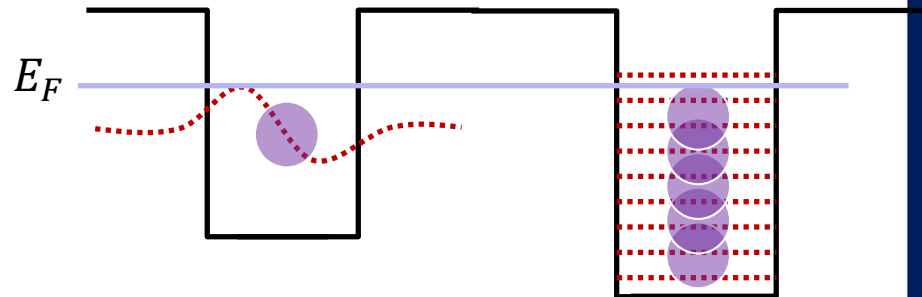
Many-body Fermi sea



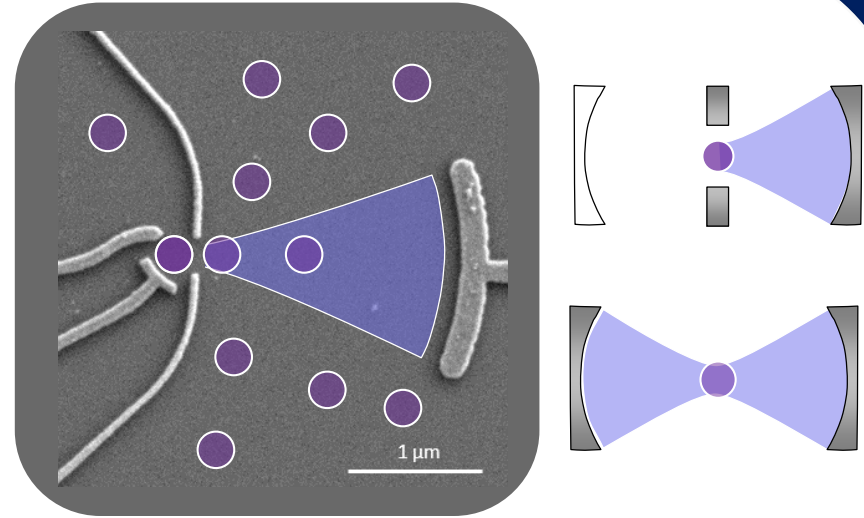
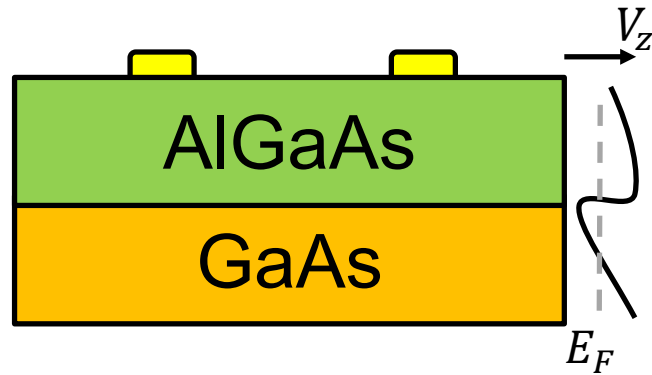
Single-particle waves



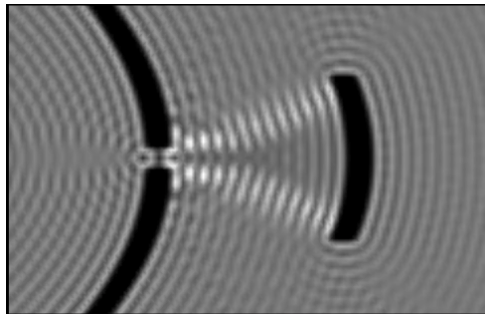
KWANT, NJP **16**, 063065 (2014)



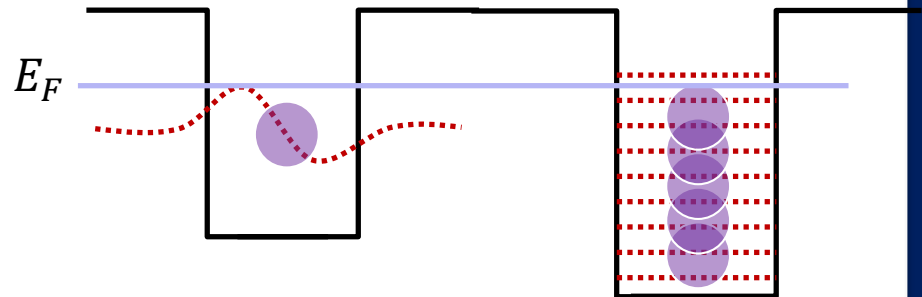
Many-body transport



Single-particle waves

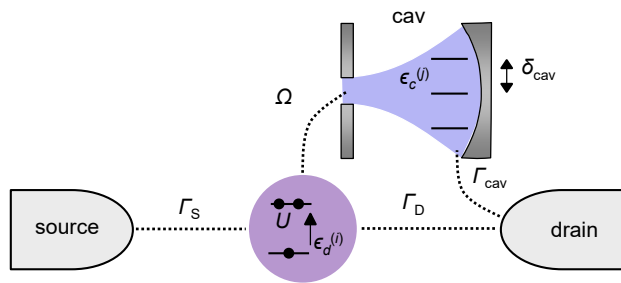
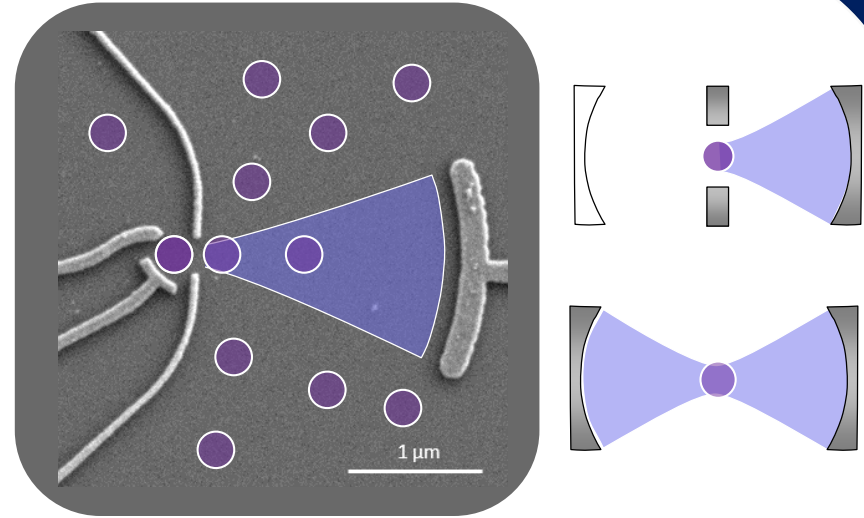
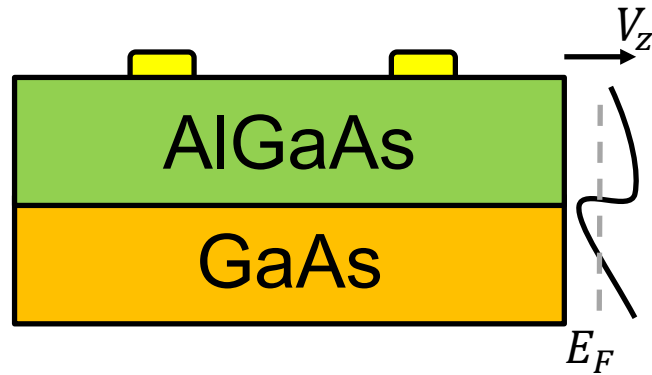


KWANT, NJP **16**, 063065 (2014)

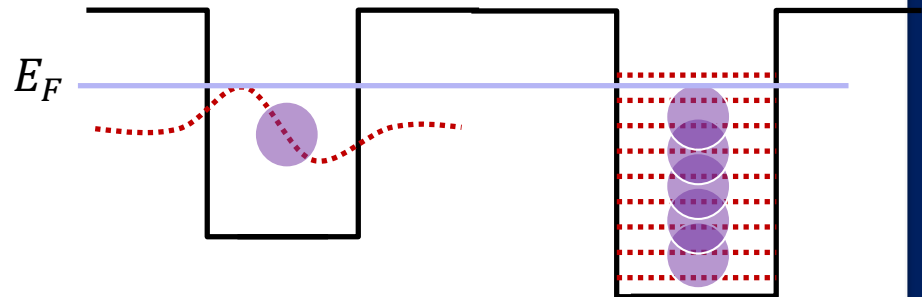


Electrons \rightarrow Spin + Interaction

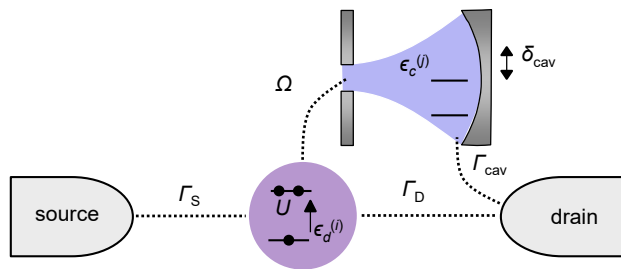
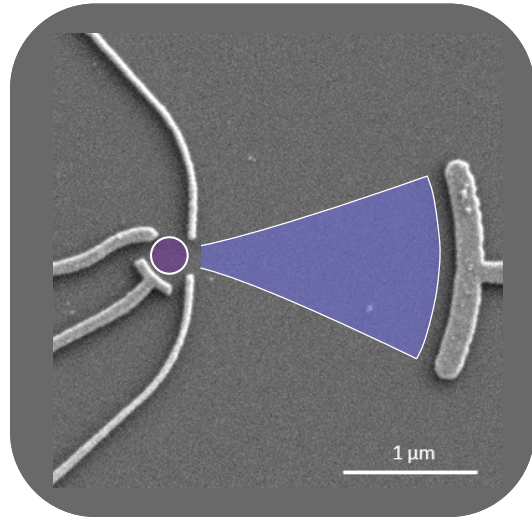
Many-body transport



Open Kondo box problem



Many-body transport



Open Kondo box problem

$$H = H_{\text{leads}} + H_{\text{dot}} + H_{\text{cav}} + H_{\text{coupl}} + H_{\text{tun}}$$

$$H_{\text{dot}} = \sum_{\sigma} \epsilon_d d_{\sigma}^{\dagger} d_{\sigma} + U n_{\uparrow} n_{\downarrow}$$

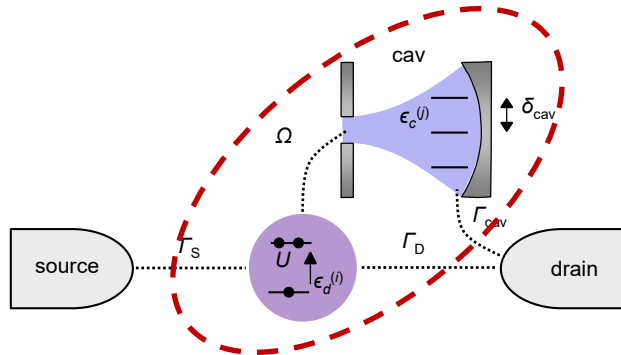
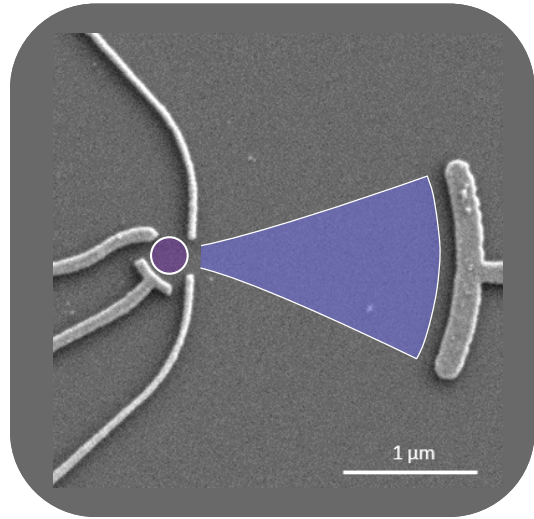
$$H_{\text{leads}} = \sum_{k,\sigma} \epsilon_{Lk} c_{Lk\sigma}^{\dagger} c_{Lk\sigma} + \sum_{k,\sigma} \epsilon_{Rk} c_{Rk\sigma}^{\dagger} c_{Rk\sigma}$$

$$H_{\text{cav}} = \sum_{\sigma,j} \epsilon_c^{(j)} f_{j\sigma}^{\dagger} f_{j\sigma}$$

$$H_{\text{coupl}} = \sum_{j,\sigma} \Omega_j f_{j\sigma}^{\dagger} d_{\sigma} + \text{h.c.}$$

$$H_{\text{tun}} = \sum_{k,\sigma} t_L d_{\sigma}^{\dagger} c_{Lk\sigma} + \text{h.c.} + \sum_{k,\sigma} t_R d_{\sigma}^{\dagger} c_{Rk\sigma} + \text{h.c.} \\ + \sum_{j,k,\sigma} t_c f_{j\sigma}^{\dagger} c_{Rk\sigma} + \text{h.c.}$$

Many-body transport



Exact diagonalization

$$H = H_{\text{leads}} + H_{\text{dot}} + H_{\text{cav}} + H_{\text{coupl}} + H_{\text{tun}}$$

$$H_{\text{dot}} = \sum_{\sigma} \epsilon_d d_{\sigma}^{\dagger} d_{\sigma} + U n_{\uparrow} n_{\downarrow}$$

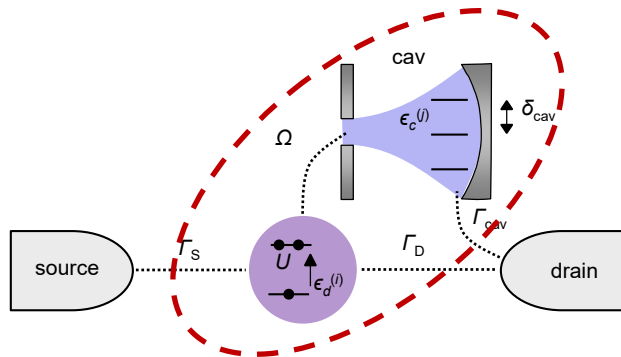
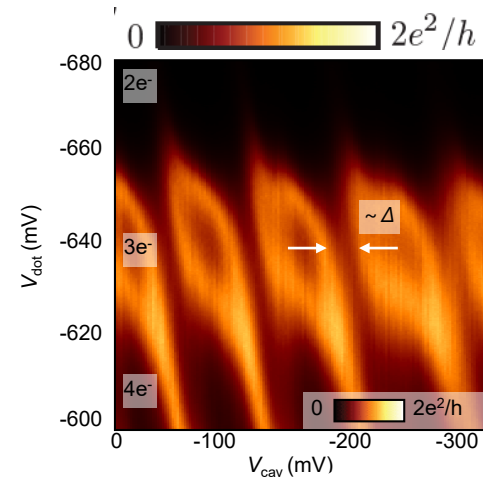
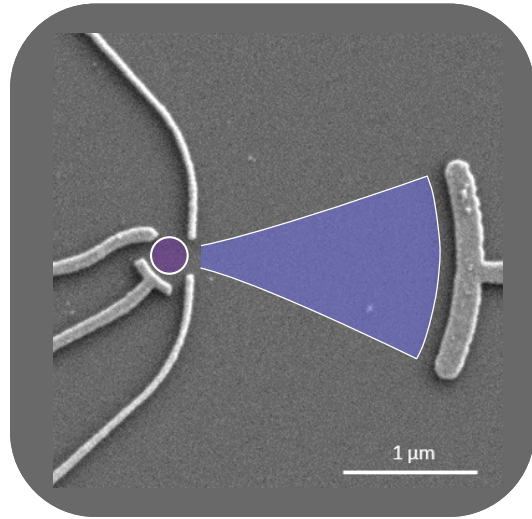
$$H_{\text{leads}} = \sum_{k,\sigma} \epsilon_{Lk} c_{Lk\sigma}^{\dagger} c_{Lk\sigma} + \sum_{k,\sigma} \epsilon_{Rk} c_{Rk\sigma}^{\dagger} c_{Rk\sigma}$$

$$H_{\text{cav}} = \sum_{\sigma,j} \epsilon_c^{(j)} f_{j\sigma}^{\dagger} f_{j\sigma}$$

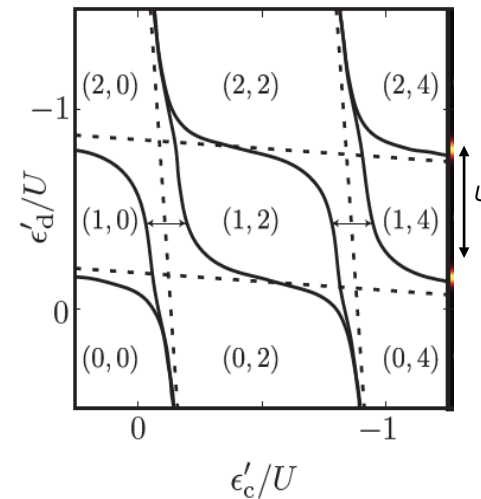
$$H_{\text{coupl}} = \sum_{j,\sigma} \Omega_j f_{j\sigma}^{\dagger} d_{\sigma} + \text{h.c.}$$

$$H_{\text{tun}} = \sum_{k,\sigma} t_L d_{\sigma}^{\dagger} c_{Lk\sigma} + \text{h.c.} + \sum_{k,\sigma} t_R d_{\sigma}^{\dagger} c_{Rk\sigma} + \text{h.c.} \\ + \sum_{j,k,\sigma} t_c f_{j\sigma}^{\dagger} c_{Rk\sigma} + \text{h.c.}$$

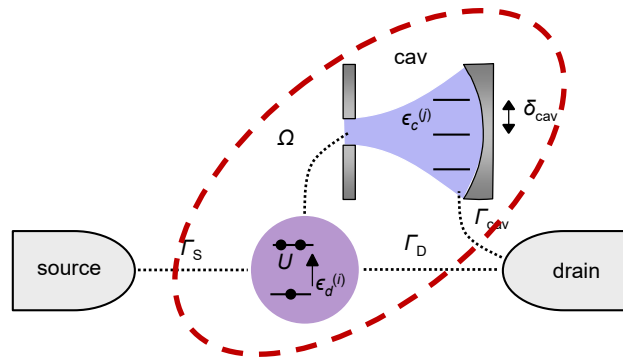
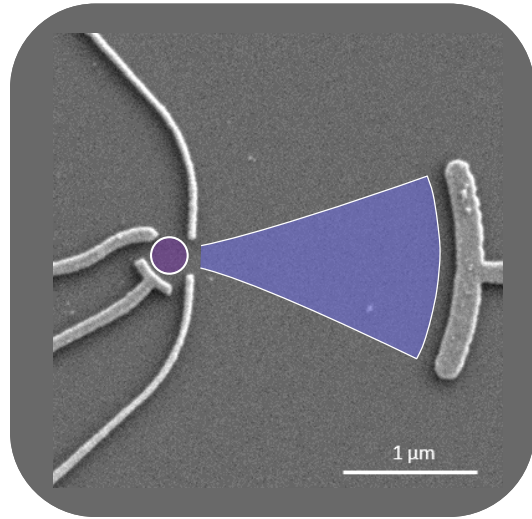
Many-body transport



Exact diagonalization



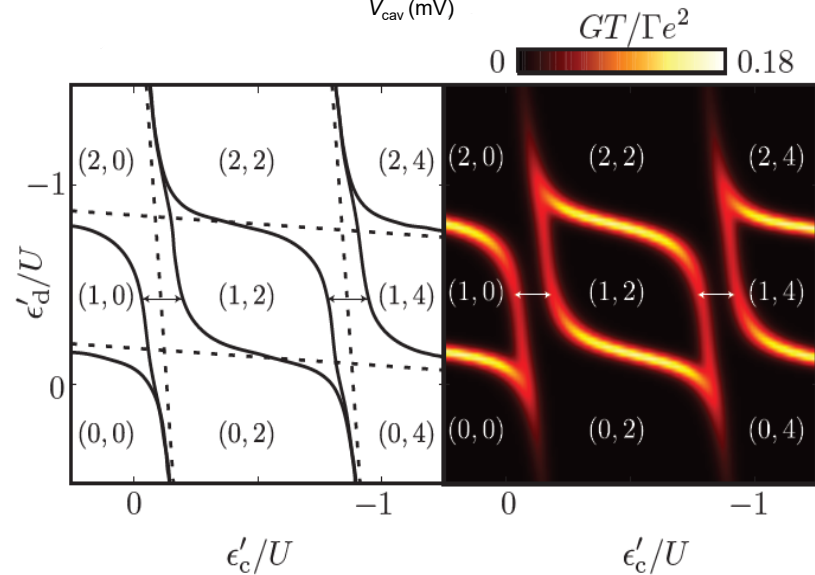
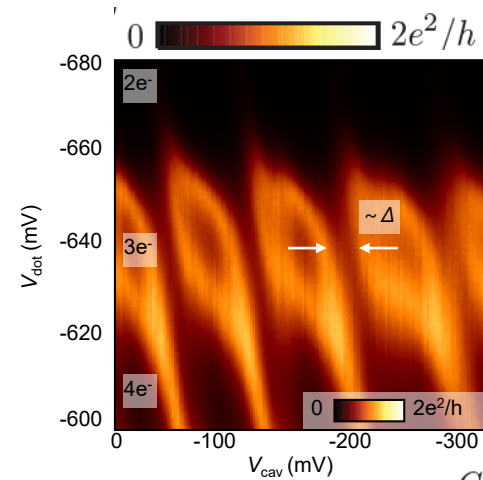
Many-body transport



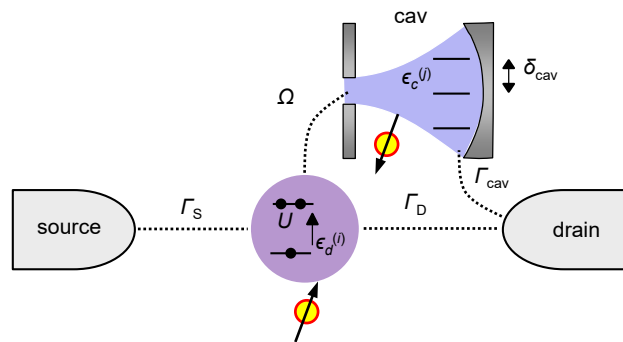
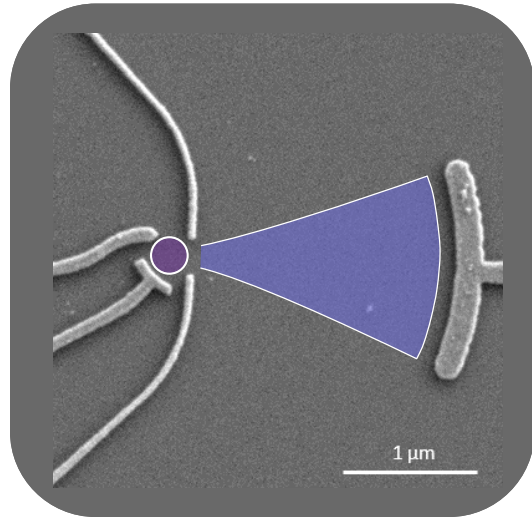
Exact diagonalization

+

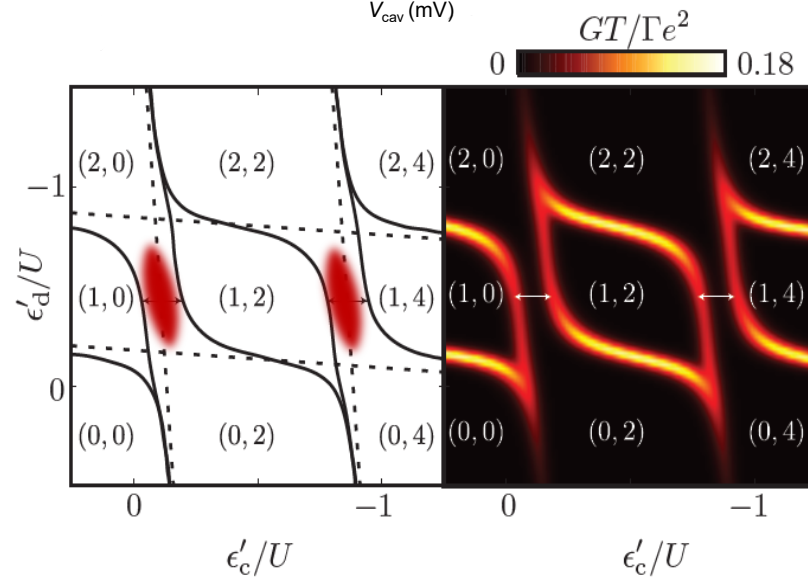
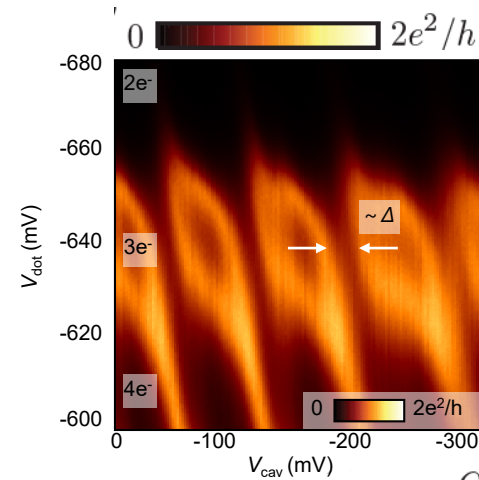
Master equation



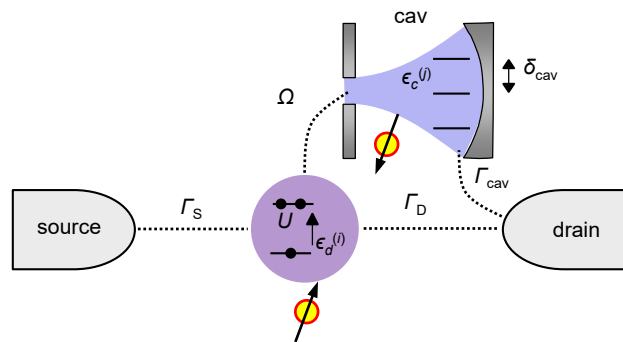
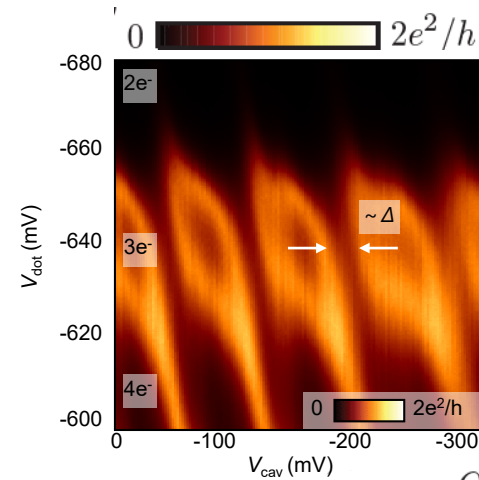
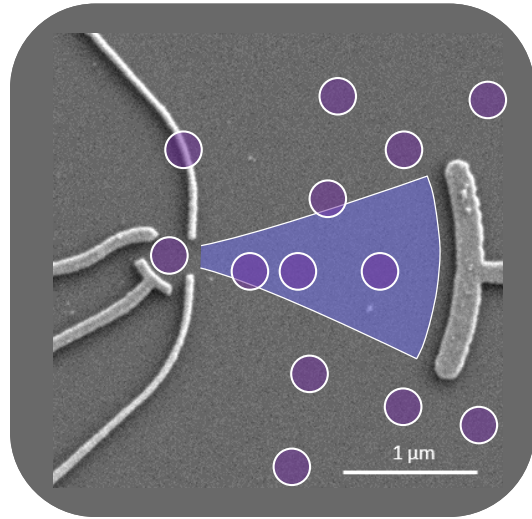
Many-body transport



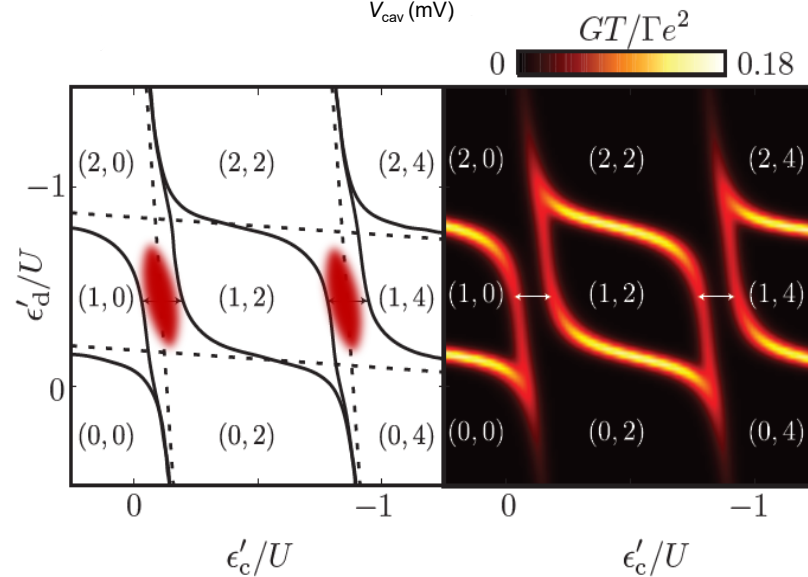
Singlet dot-cavity
molecule



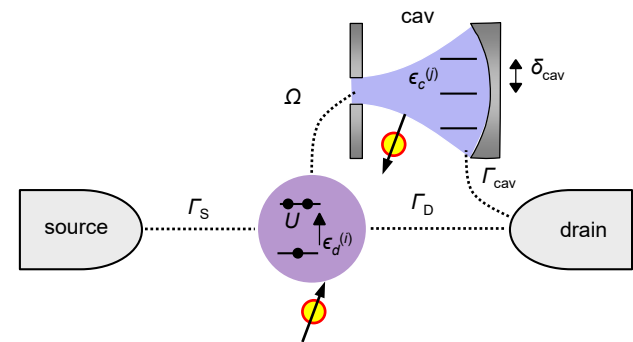
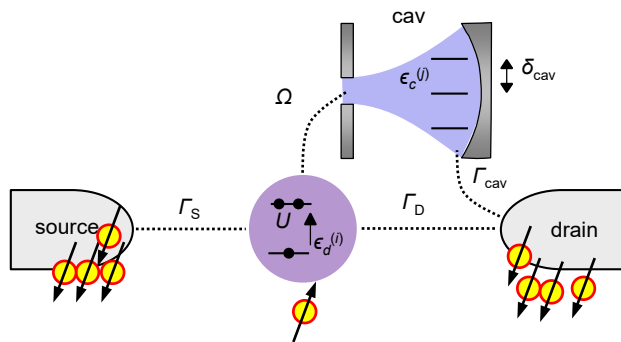
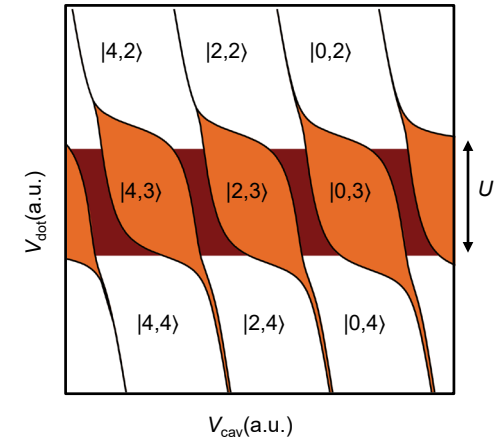
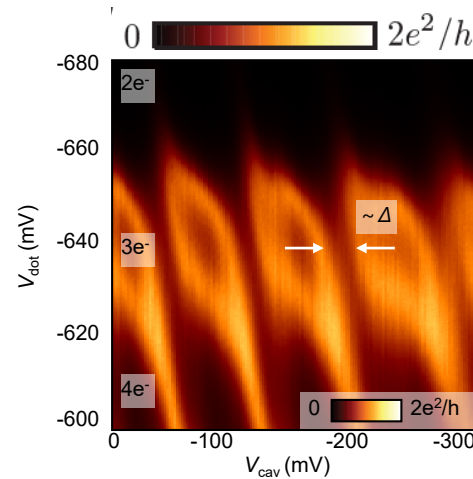
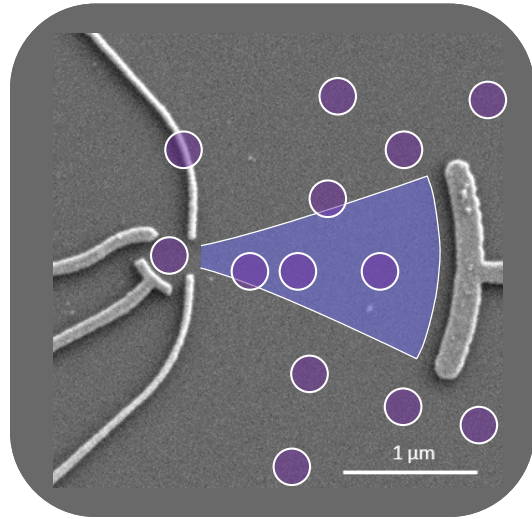
Many-body transport



Singlet dot-cavity
molecule



Many-body transport



Many-body Kondo singlet

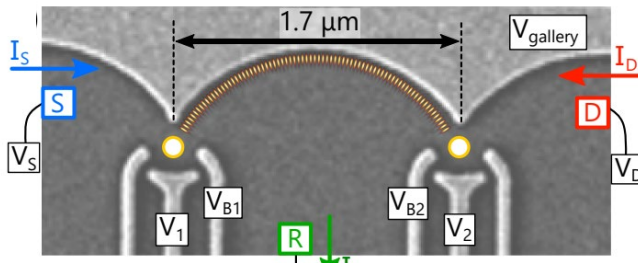
Singlet dot-cavity molecule

QUEST research

Quantum engineering of

Devices

Mesoscopic transport



engineered quantum chemistry

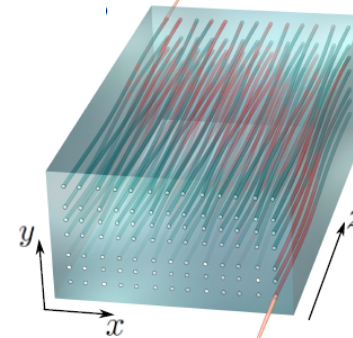


many-body cond. mat.

- Electronic interferometers
- Kondo impurities ←
- Quantum measurement
- Topological semimetals

Material properties

Quantum simulation



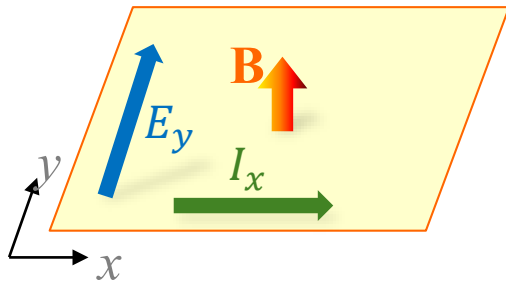
designer models



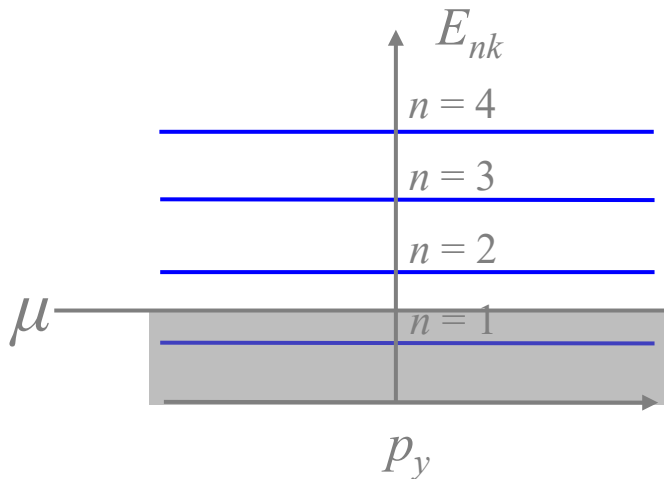
real materials

- Topological photonics
- Synthetic dimensions ←
- Quasicrystals
- Dissipative phase transitions

2D quantum Hall effect



K. Von Klitzing, RMP 58, 519 (1986).



Berry curvature

$$\Omega_n(\mathbf{k}) = i \left(\left\langle \partial_{k_y} u_n(\mathbf{k}) \middle| \partial_{k_x} u_n(\mathbf{k}) \right\rangle - \left\langle \partial_{k_x} u_n(\mathbf{k}) \middle| \partial_{k_y} u_n(\mathbf{k}) \right\rangle \right)$$

quantized transverse linear response

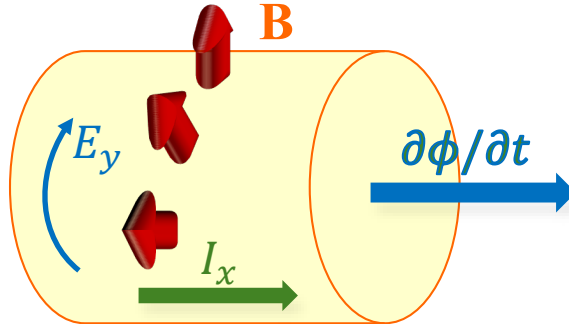
$$\sigma_{xy} \equiv \frac{I_x}{E_y} = \frac{e^2}{h} \sum_i^{\mu} C_i$$

1st Chern number

$$C_n = \frac{1}{2\pi} \iint_{BZ} \Omega_n(\mathbf{k}) dk^2$$

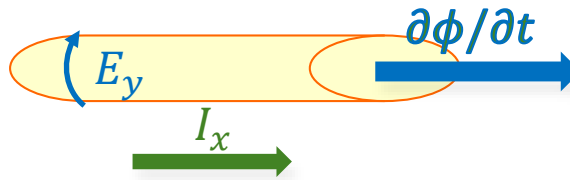
Topological pumps

$$\sigma_{xy} \equiv \frac{I_x}{E_y} = \frac{e^2}{h} \sum_i^{\mu} C_i$$



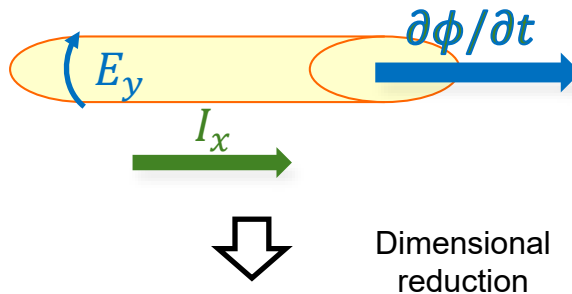
Topological pumps

$$\sigma_{xy} \equiv \frac{I_x}{E_y} = \frac{e^2}{h} \sum_i^{\mu} C_i$$

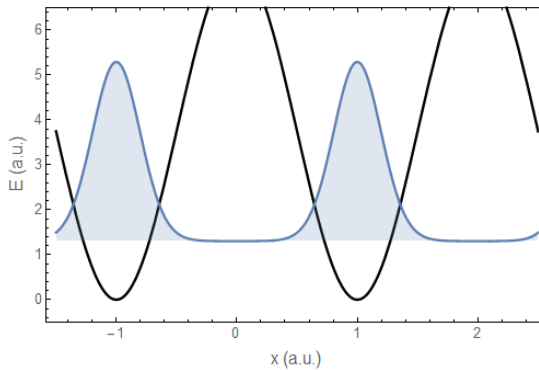


Topological pumps

$$\sigma_{xy} \equiv \frac{I_x}{E_y} = \frac{e^2}{h} \sum_i^{\mu} C_i$$

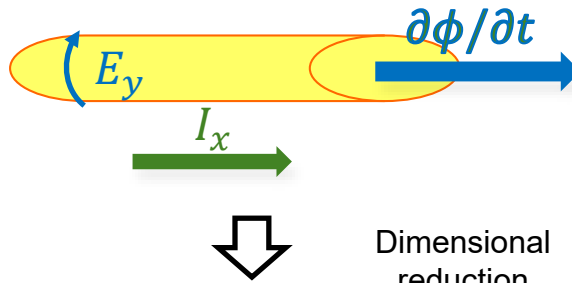


Laughlin, PRB 23,
 5632 (1981)
 Thouless PRB 27,
 6083 (1983)

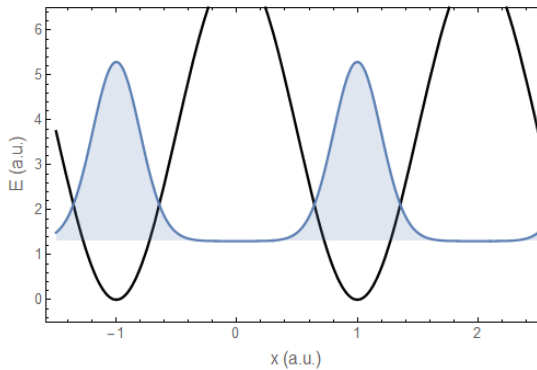


Topological pumps

$$\sigma_{xy} \equiv \frac{I_x}{E_y} = \frac{e^2}{h} \sum_i^{\mu} C_i$$



Laughlin, PRB 23,
 5632 (1981)
 Thouless PRB 27,
 6083 (1983)

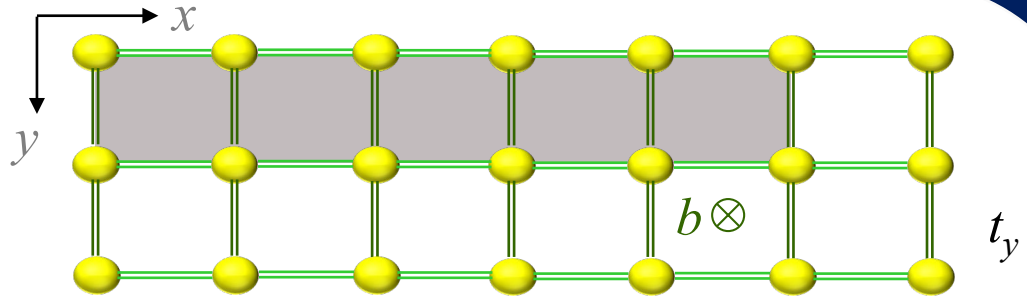


$$\langle x \rangle = \iint \langle v_n(k_x, t) \rangle dk_x dt = C_n d_1$$

$$C_n = \frac{1}{2\pi} \iint \Omega_n(k_x, \phi) dk_x d\phi$$

Hofstadter model

- Hamiltonian:



$$\begin{aligned} \mathcal{H} &= \sum_{x,y} t_x (c_{x,y}^\dagger c_{x+1,y} + h.c.) + t_y (e^{i2\pi bx} c_{x,y}^\dagger c_{x,y+1} + h.c.) \\ &= \sum_{x,k_y} t (c_{x,k_y}^\dagger c_{x+1,k_y} + h.c.) + 2t_y \cos(2\pi bx + k_y) c_{x,k_y}^\dagger c_{x,k_y} \end{aligned}$$

- Spectrum:

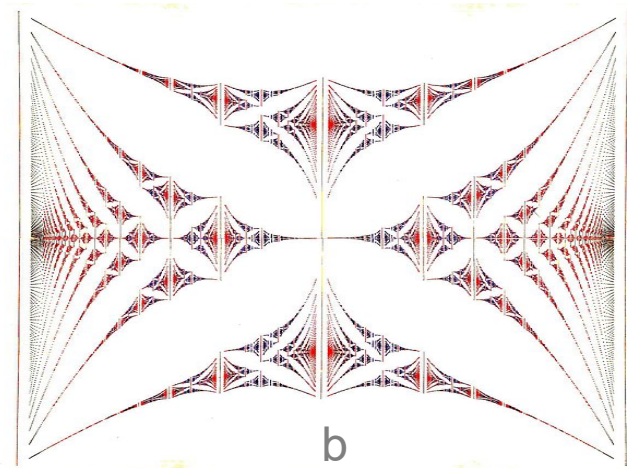
Harper, PPSL A **68**, 874 (1955)

Azbel, JETP **19**, 634 (1964)

Hofstadter, PRB **14**, 2239 (1976)

$$b = \frac{p}{q}$$

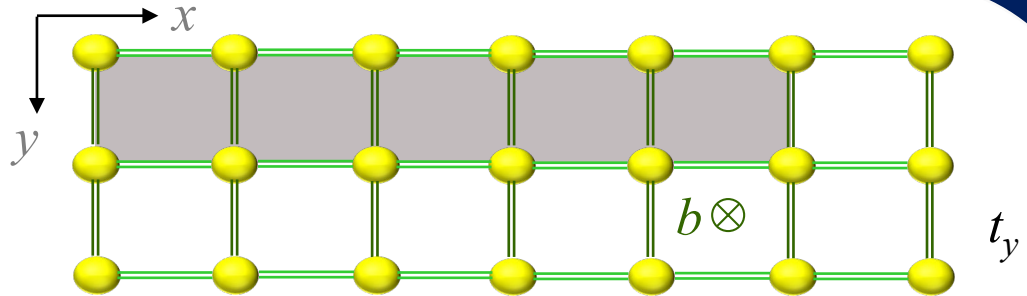
$$c_{x,y} = \sum_{k_y} e^{ik_y y} \tilde{c}_x$$



Hofstadter model

- Hamiltonian:

$$\mathcal{H} = \sum_{x,k_y} t_x \left(c_{x,k_y}^\dagger c_{x+1,k_y} + h.c. \right) + 2t_y \cos(2\pi b x + k_y) c_{x,k_y}^\dagger c_{x,k_y}$$



- Quantized Hall conductance:

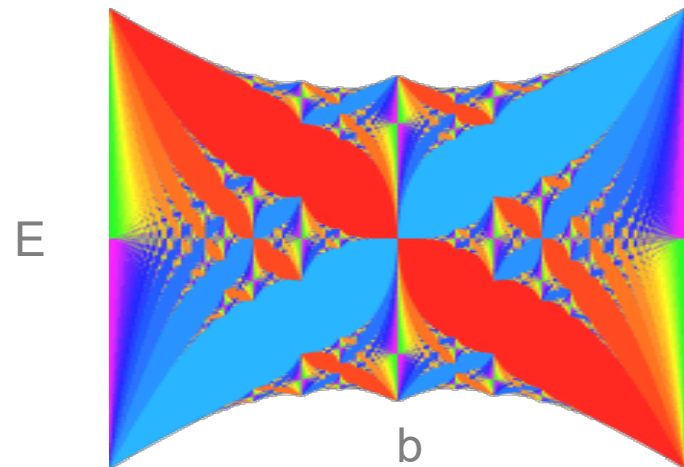
TKNN, PRL **49**, 405 (1982)

$$\sigma_{xy} = \nu \frac{e^2}{h}$$

- Chern numbers:

$$\nu = \int_0^{2\pi} dp_x \int_0^{2\pi} dp_y \Omega(p_x, p_y)$$

D. Osadchy and J. E. Avron, J. Math. Phys. **42**, 5665 (2001)



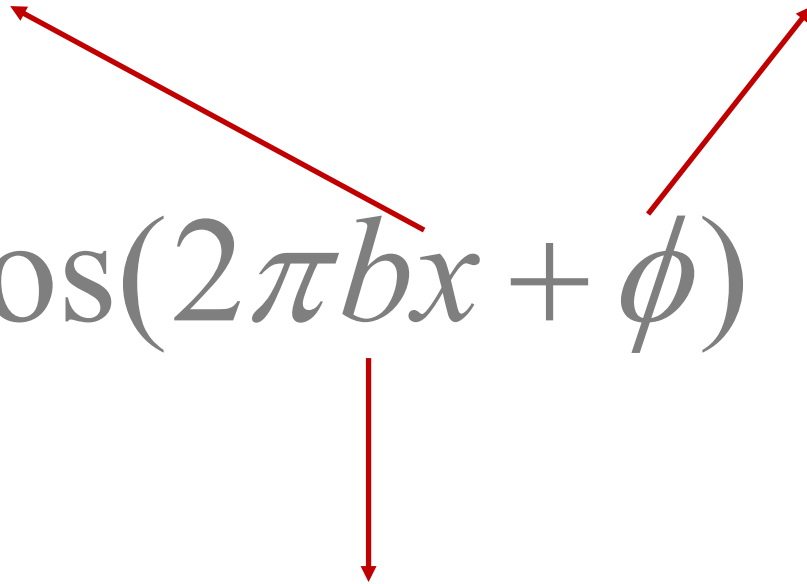
Dimensional reduction, pumps, and quasicrystals

Real dimension

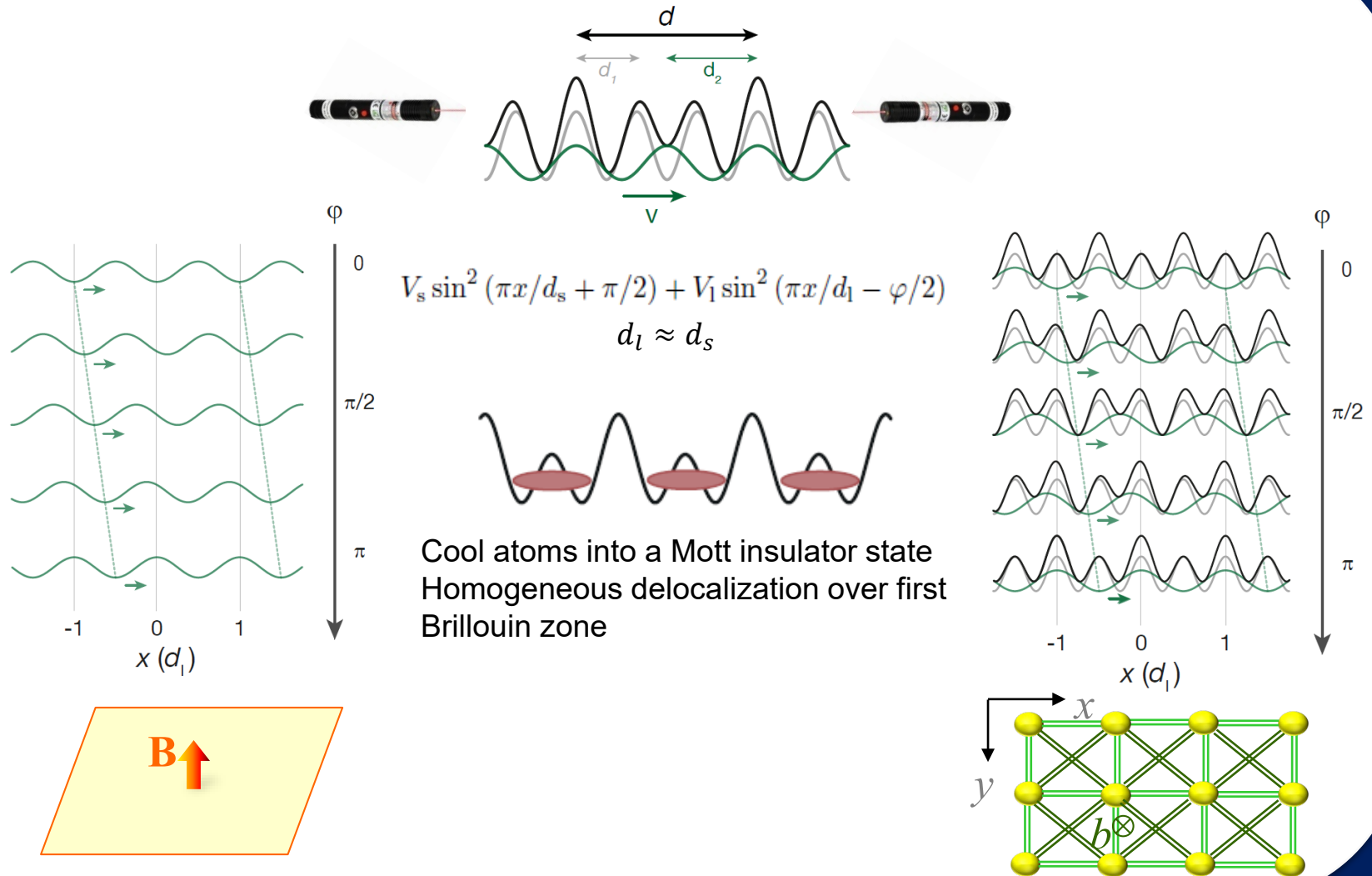
Synthetic dimension

$$\cos(2\pi bx + \phi)$$

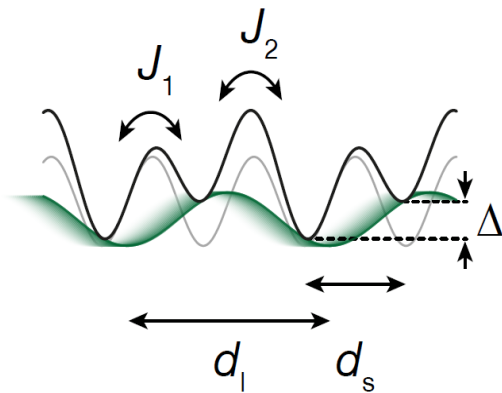
“Long-range” order



Atomic topological pumps

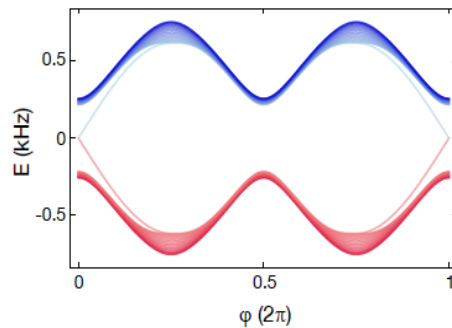


Atomic topological pumps

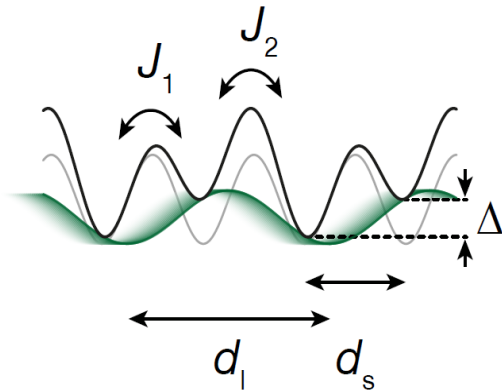


Rice-Mele Model [PRL 49, 1455 (1982)]

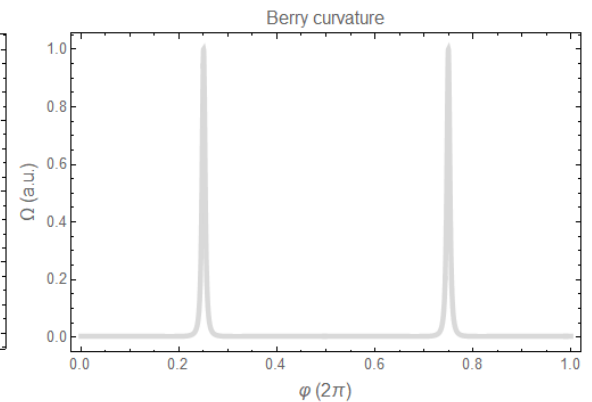
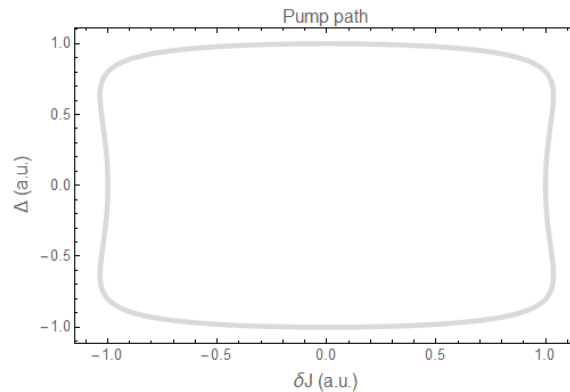
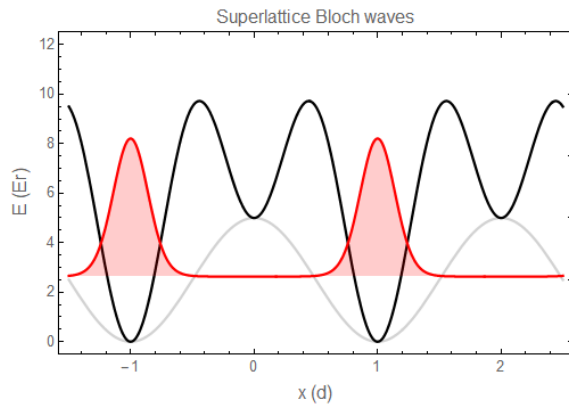
$$\hat{H}(\varphi) = - \sum_m \left(J_1(\varphi) \hat{b}_m^\dagger \hat{a}_m + J_2(\varphi) \hat{a}_{m+1}^\dagger \hat{b}_m + \text{h.c.} \right) + \frac{\Delta(\varphi)}{2} \sum_m \left(\hat{a}_m^\dagger \hat{a}_m - \hat{b}_m^\dagger \hat{b}_m \right)$$



Atomic topological pumps

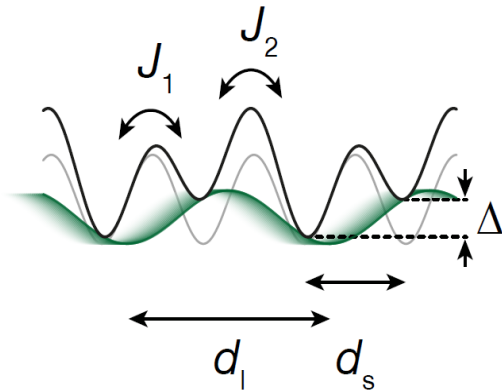


$$\hat{H}(\varphi) = - \sum_m \left(J_1(\varphi) \hat{b}_m^\dagger \hat{a}_m + J_2(\varphi) \hat{a}_{m+1}^\dagger \hat{b}_m + \text{h.c.} \right) + \frac{\Delta(\varphi)}{2} \sum_m \left(\hat{a}_m^\dagger \hat{a}_m - \hat{b}_m^\dagger \hat{b}_m \right)$$



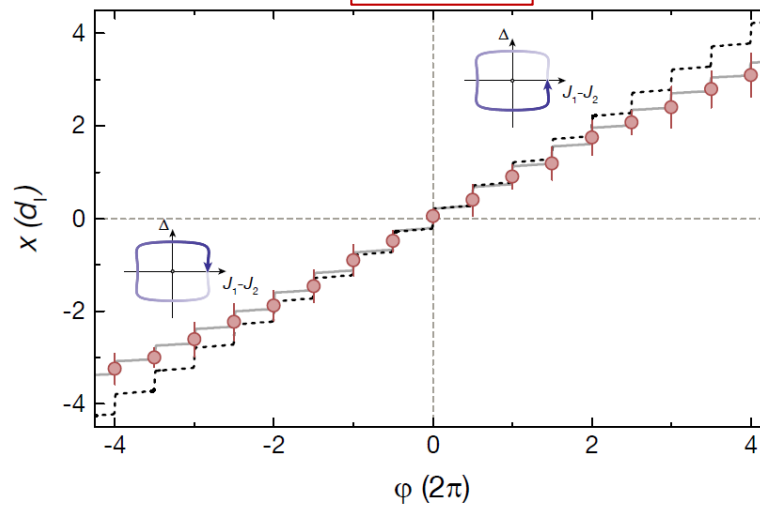
$$\langle x \rangle = \iint \langle v_n(k_x, t) \rangle dk_x dt = C_n d_1$$

Atomic topological pumps

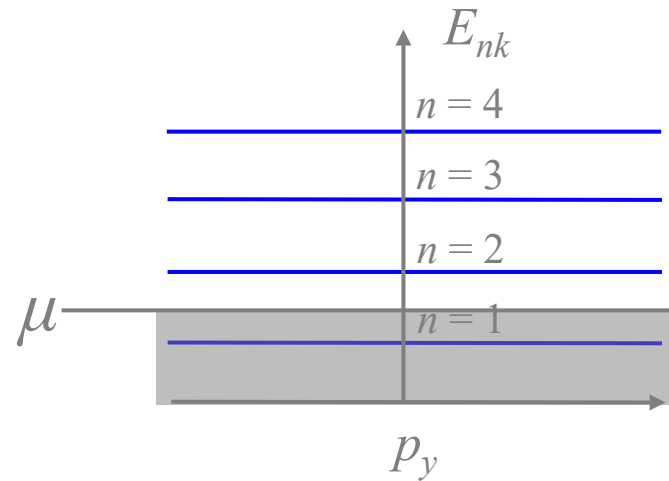


$$\hat{H}(\varphi) = - \sum_m \left(J_1(\varphi) \hat{b}_m^\dagger \hat{a}_m + J_2(\varphi) \hat{a}_{m+1}^\dagger \hat{b}_m + \text{h.c.} \right) + \frac{\Delta(\varphi)}{2} \sum_m \left(\hat{a}_m^\dagger \hat{a}_m - \hat{b}_m^\dagger \hat{b}_m \right)$$

$$C_1 = +1$$



4D quantum Hall effect



$$I_\alpha = \chi \frac{e^2}{h} \varepsilon_{\alpha\beta\gamma\delta} \frac{B_{\beta\gamma}}{\Phi_0} E_\delta;$$

$$\chi = \frac{1}{(2\pi)^2} \iiint_{BZ} dk_x dk_y dk_z dk_w \Omega \wedge \Omega$$

First derivations:

J. E. Avron *et al.*, *Comm. Math. Phys.* 124, 595 (1989).

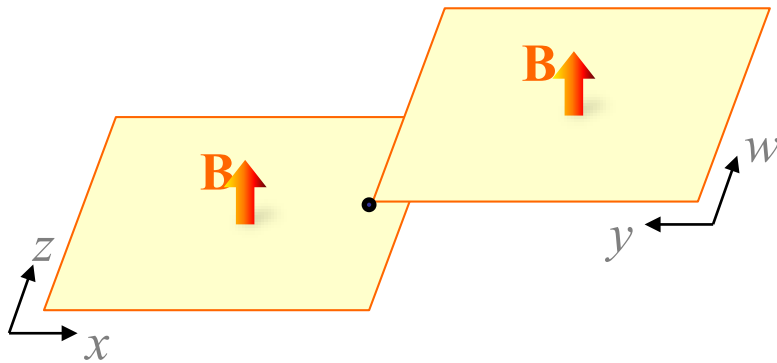
J. Fröhlich and B. Perdini, in *Mathematical Physics 2000* (Imperial College Press, London, United Kingdom)..

S.-C. Zhang and J. Hu, *Science* Vol. 294, 823 (2001):

X.-L. Qi and S.-C. Zhang, *Rev. Mod. Phys.* 83, 1057 (2011).

4D quantum Hall effect

K. Kraus, Z. Ringel, and OZ, PRL **111**, 226401 (2013)

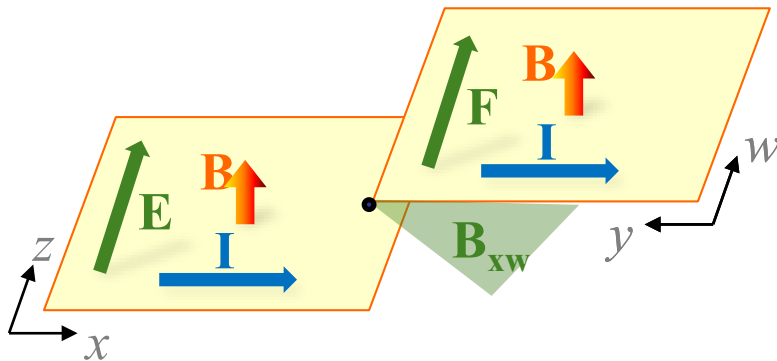


$$I_{\alpha} = \chi \frac{e^2}{h} \varepsilon_{\alpha\beta\gamma\delta} \frac{B_{\beta\gamma}}{\Phi_0} E_{\delta};$$

$$\chi = \frac{1}{(2\pi)^2} \iiint \iiint_{BZ} dk_x dk_y dk_z dk_w \Omega_{xz} \Omega_{yw}$$

4D quantum Hall effect

K. Kraus, Z. Ringel, and OZ, PRL **111**, 226401 (2013)



$$I_y = \chi \frac{e^2}{h} \varepsilon_{x\beta\gamma\delta} \frac{B_{\beta\gamma}}{\Phi_0} E_\delta;$$

Lorentz-type response

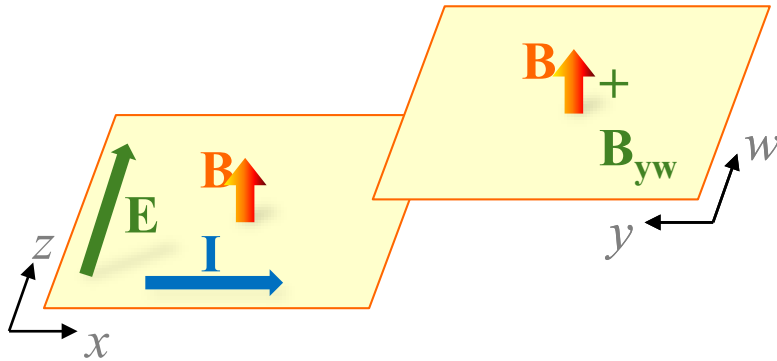
$$I_v = I_w = 0$$

$$I_x = \frac{e^2}{h} n_{yw} v_{xz} E_z;$$

$$I_y = \chi \frac{e^2}{h} \frac{B_{xw}}{\Phi_0} E_z$$

4D quantum Hall effect

K. Kraus, Z. Ringel, and OZ, PRL **111**, 226401 (2013)



$$I_y = \chi \frac{e^2}{h} \varepsilon_{x\beta\gamma\delta} \frac{B_{\beta\gamma}}{\Phi_0} E_\delta;$$

Lorentz-type response

$$I_v = I_w = 0$$

$$I_x = \frac{e^2}{h} n_{yw} v_{xz} E_z;$$

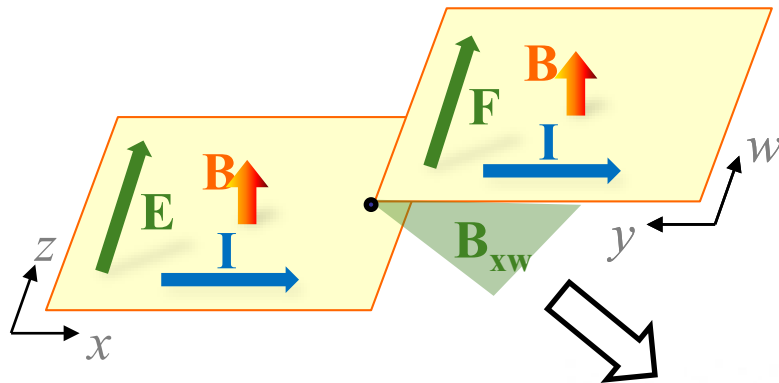
$$I_y = \chi \frac{e^2}{h} \frac{B_{xw}}{\Phi_0} E_z$$

Density-type response

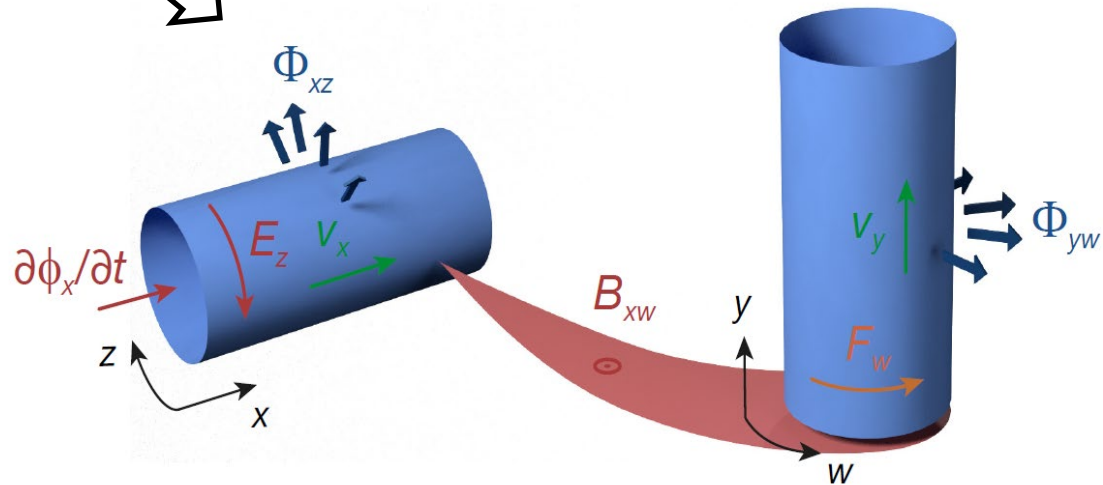
$$I_v = I_y = I_w = 0$$

$$I_x = \chi \frac{e^2}{h} \frac{B_{yw}}{\Phi_0} E_v + \frac{e^2}{h} v_{xv} n_{yw} E_v;$$

2D topological charge pump



$$I_y = \chi \frac{e^2}{h} \frac{B_{xw}}{\Phi_0} E_z;$$



Dimensional reduction, pumps, and quasicrystals

Real dimension

Synthetic dimension

$$\cos(2\pi bx + \phi)$$

+

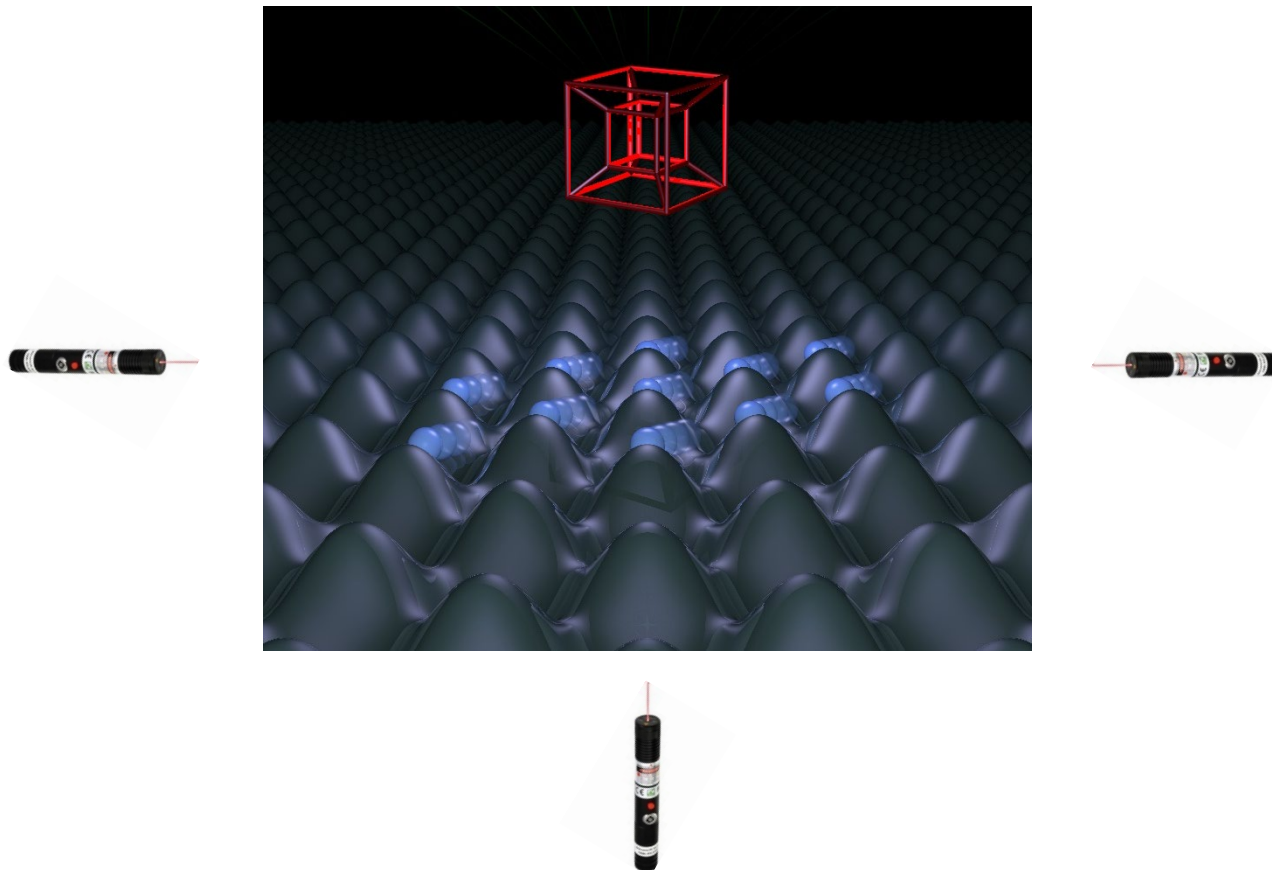
$$\cos(2\pi by + \varphi)$$

Real dimension

Synthetic dimension

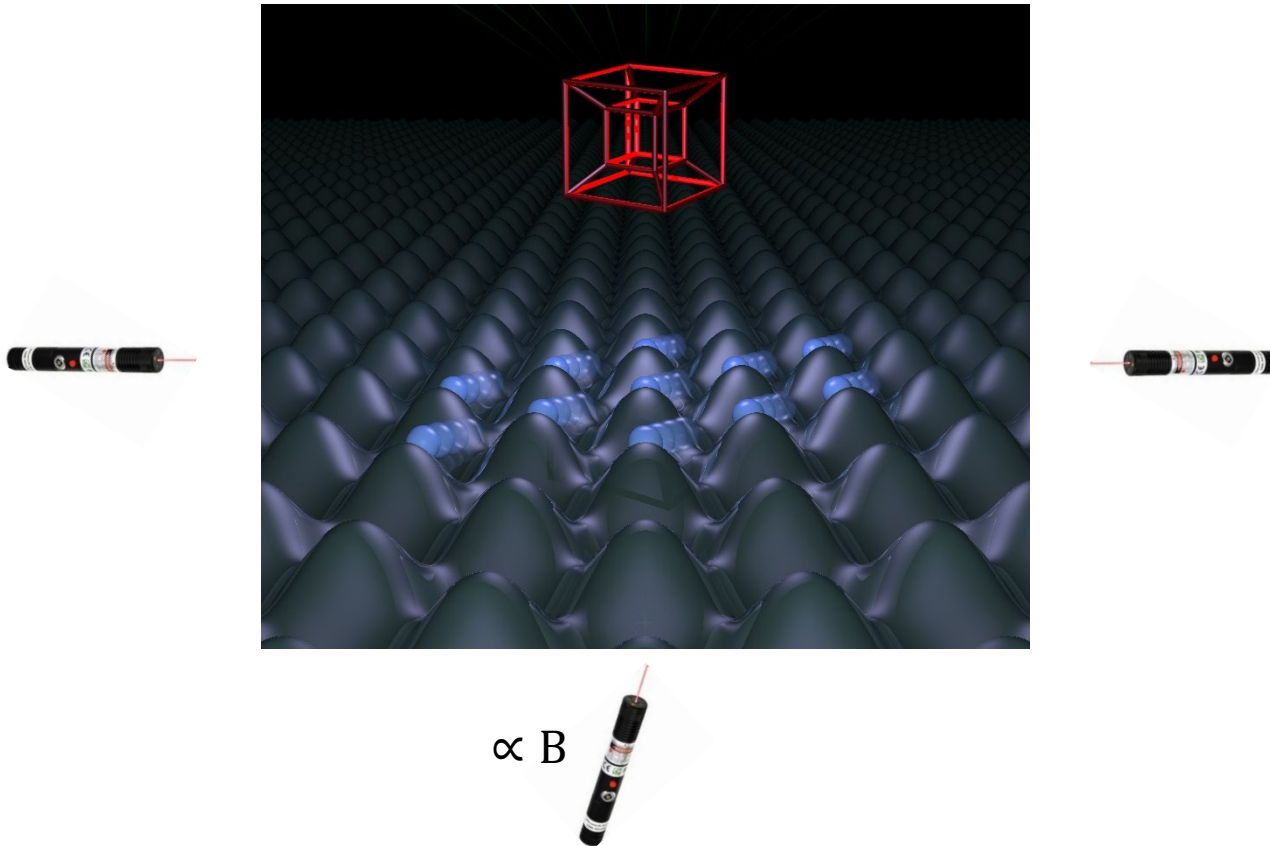
2D topological charge pump

- An optical superlattice



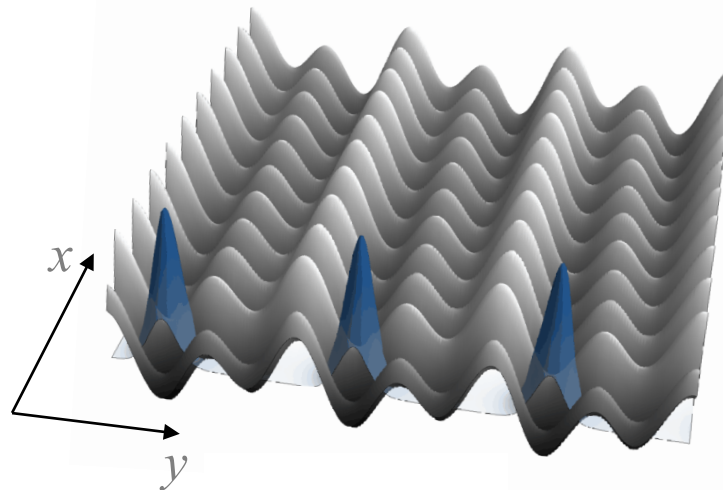
2D topological charge pump

- An optical superlattice

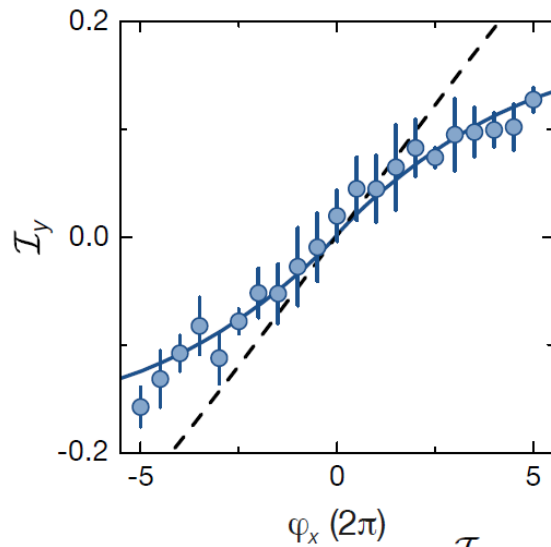


2D topological charge pump

$$I_y = \chi \frac{e^2}{h} \frac{B_{xw}}{\Phi_0} E_z;$$

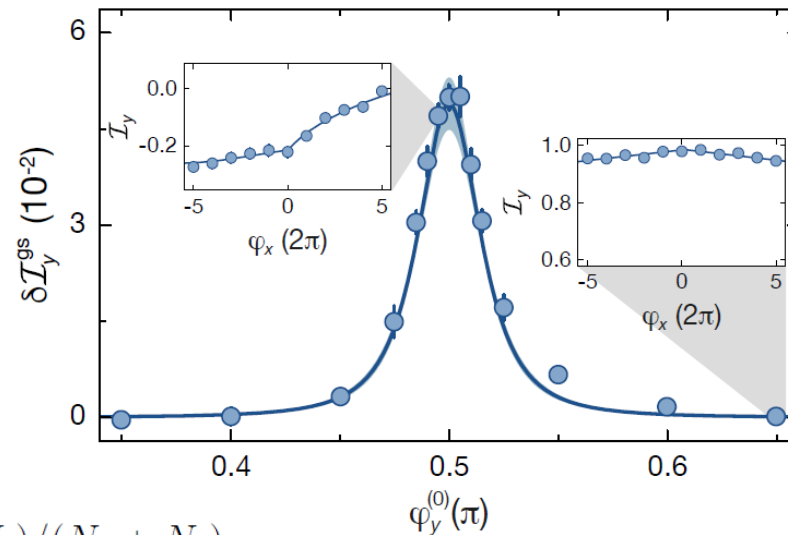


$$\chi = 1.07(8)$$



$\varphi_x (2\pi)$

$$I_y = (N_o - N_e)/(N_o + N_e)$$



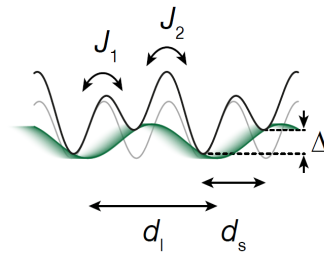
$\varphi_y^{(0)} (\pi)$

Boundary effects in photonics

Topological pumps

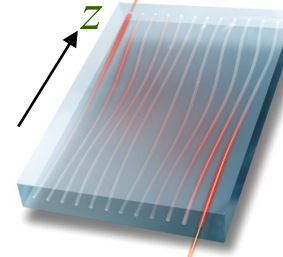
1+1D

Bulk (cold atoms)



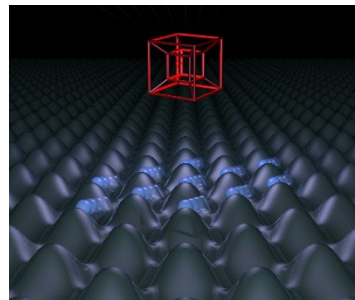
Nat. Phys. 12, 350 (2016)

Boundary (photons)

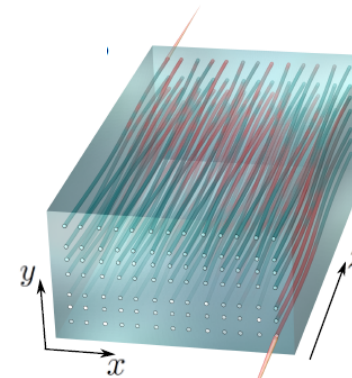


Phys. Rev. Lett. 109, 106402 (2012)

2+2D



Nature 553, 55 (2018)



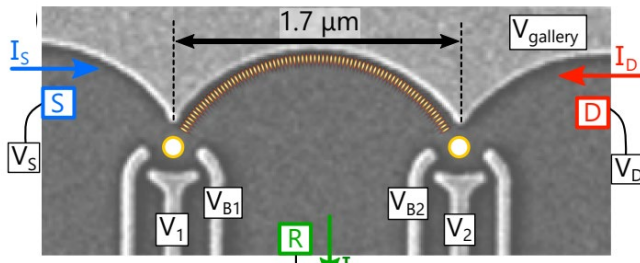
Nature 553, 59 (2018)

QUEST research

Quantum engineering of

Devices

Mesoscopic transport



engineered quantum chemistry

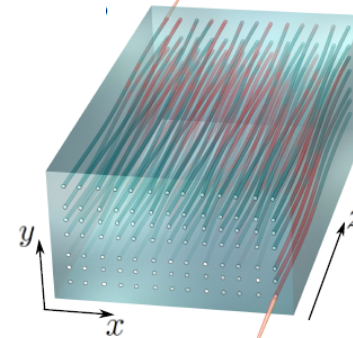


many-body cond. mat.

- Electronic interferometers
- Kondo impurities ←
- Quantum measurement
- Topological semimetals

Material properties

Quantum simulation



designer models

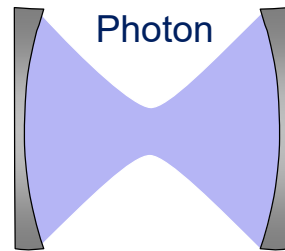


real materials

- Topological photonics
- Synthetic dimensions ←
- Quasicrystals
- Dissipative phase transitions

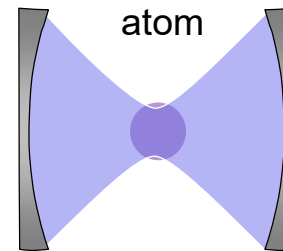
Particle in a box

Optical resonators

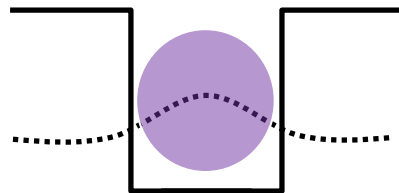


RMP **85**, 1083 (2013)

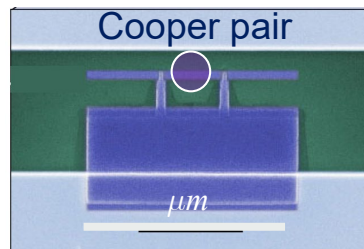
Optical cavities



RMP **85**, 1083 (2013)

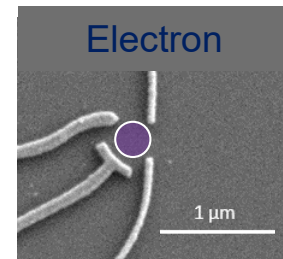


Superconducting loops



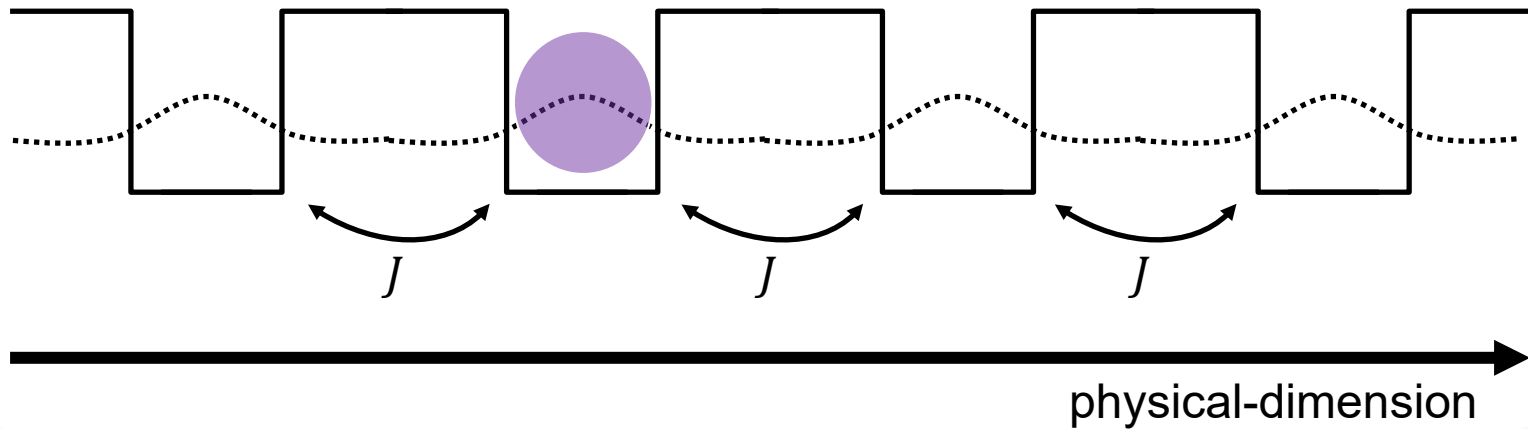
Nature **431**, 162 (2004)

Quantum dots

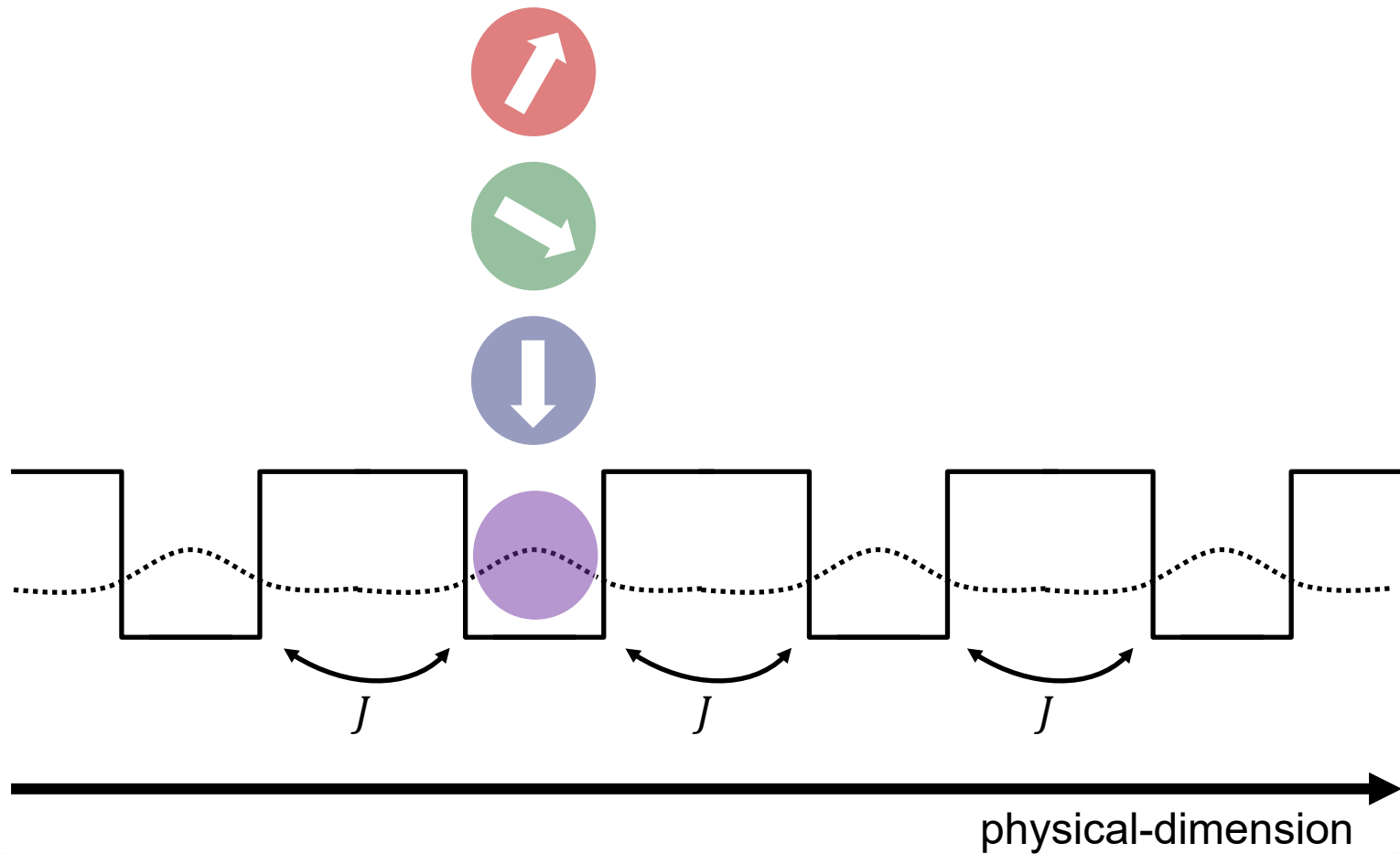


PRL **115**, 166603 (2015)

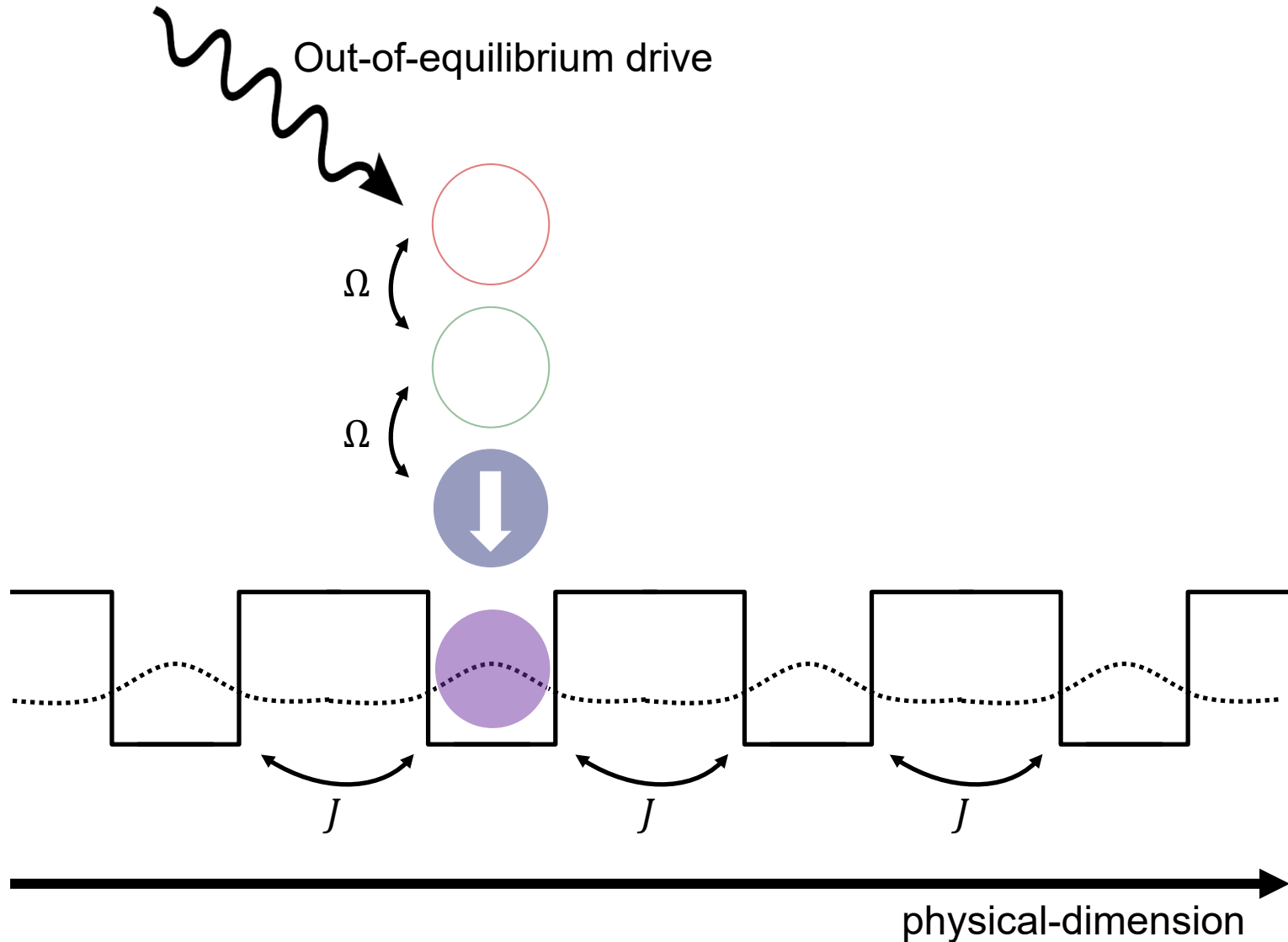
Quantum simulation



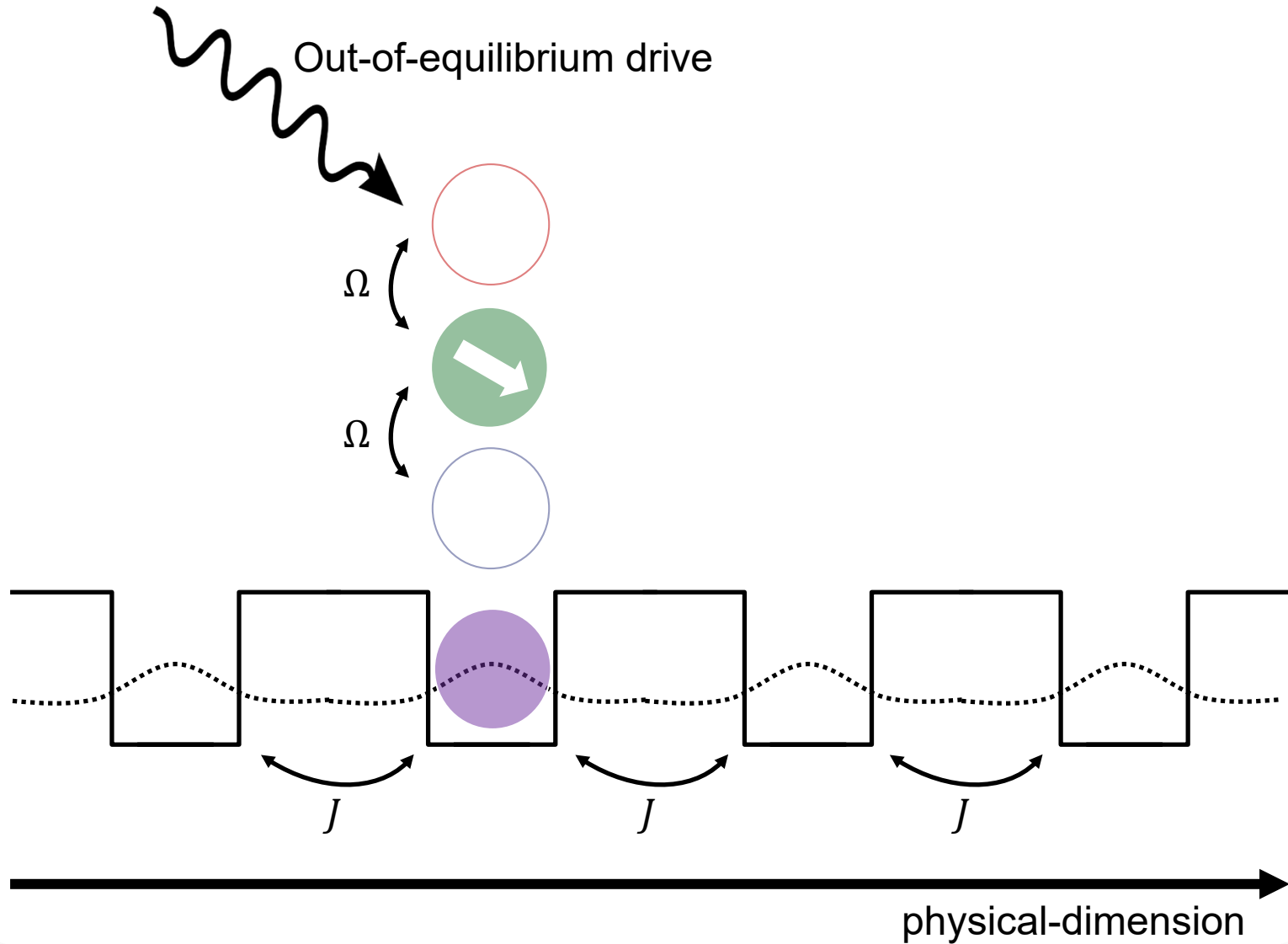
Synthetic dimensions



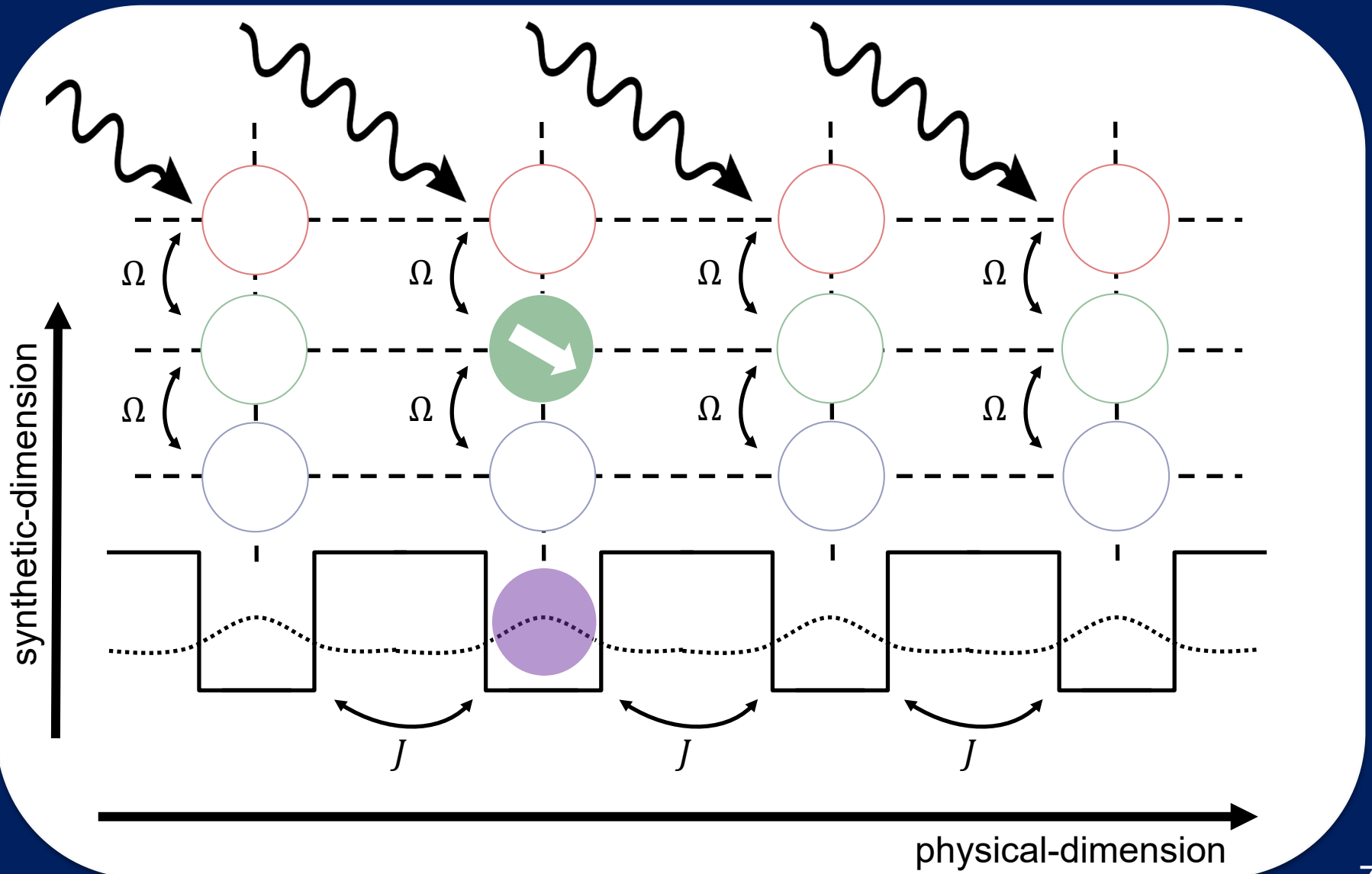
Synthetic dimensions



Synthetic dimensions

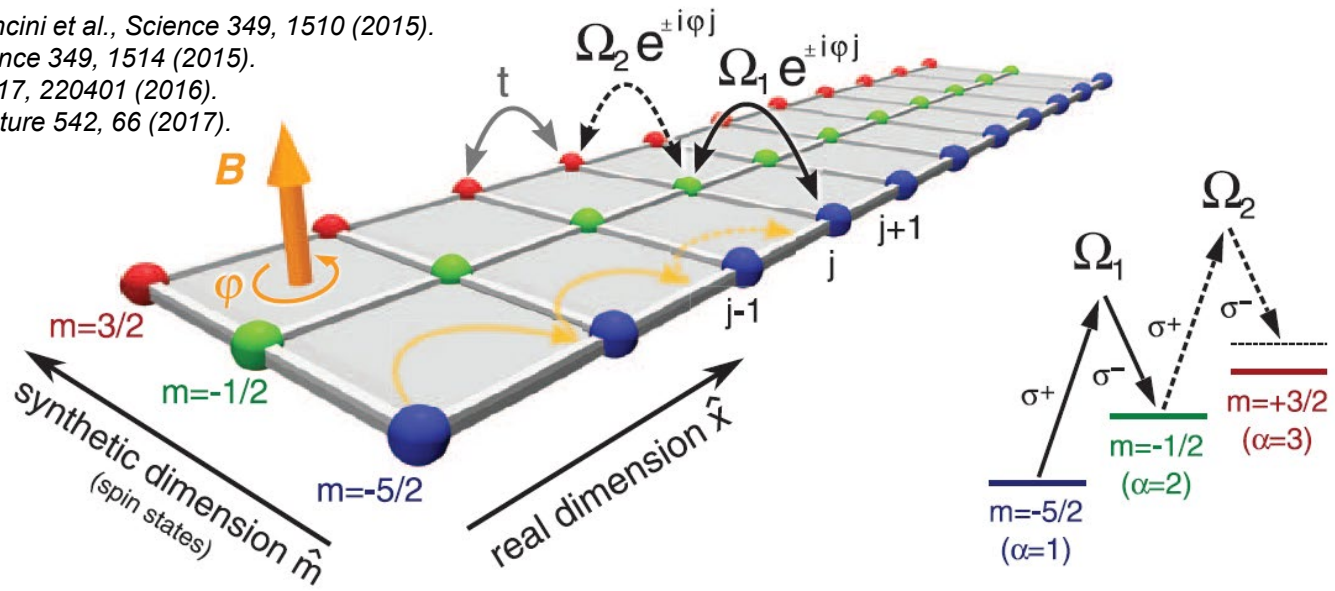


1 Synthetic + 1 physical dimensions



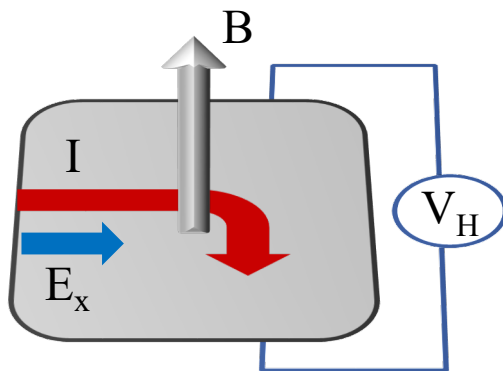
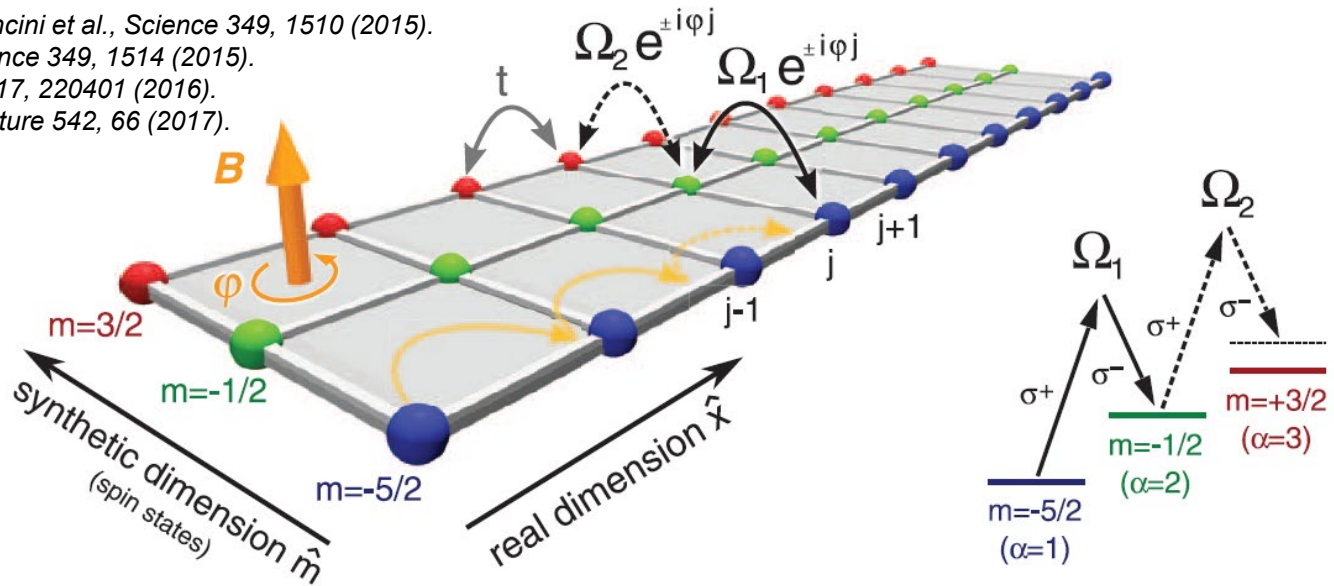
Recent experimental realizations

Image source: M. Mancini et al., *Science* 349, 1510 (2015).
 B. K. Stuhl et al., *Science* 349, 1514 (2015).
 L. F. Livi et al., *PRL* 117, 220401 (2016).
 S. Kolkowitz et al., *Nature* 542, 66 (2017).



(1+1)D quantum Hall effect

Image source: M. Mancini et al., *Science* 349, 1510 (2015).
 B. K. Stuhl et al., *Science* 349, 1514 (2015).
 L. F. Livi et al., *PRL* 117, 220401 (2016).
 S. Kolkowitz et al., *Nature* 542, 66 (2017).



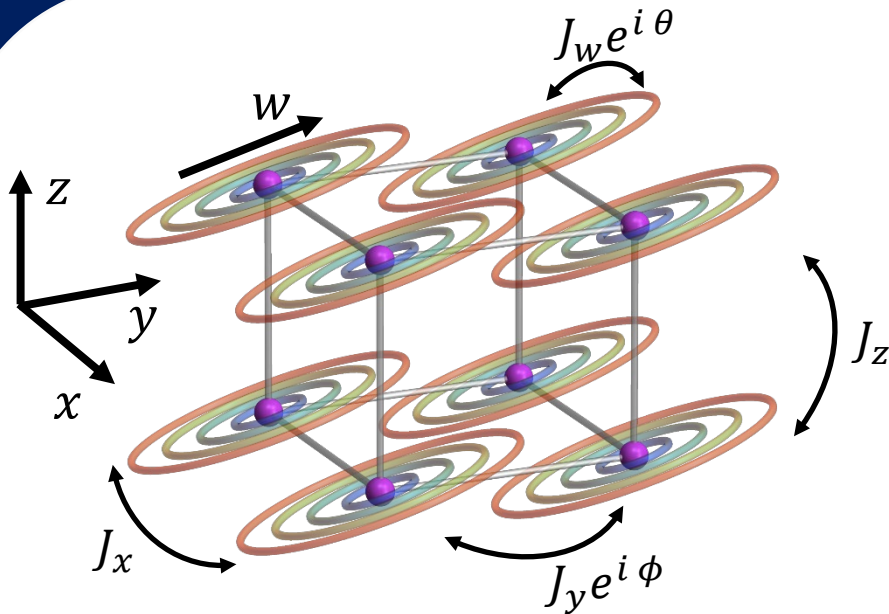
K. Von Klitzing, *RMP* 58, 519 (1986).

quantized transverse linear response

$$I_y = C_1 \frac{e^2}{h} E_x$$

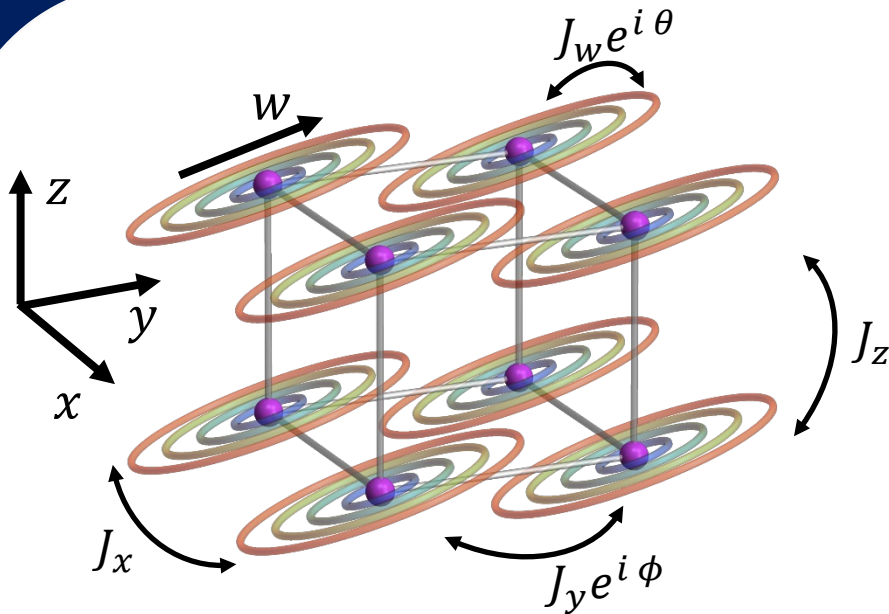
1st Chern number

1 Synthetic + 3 physical dimensions

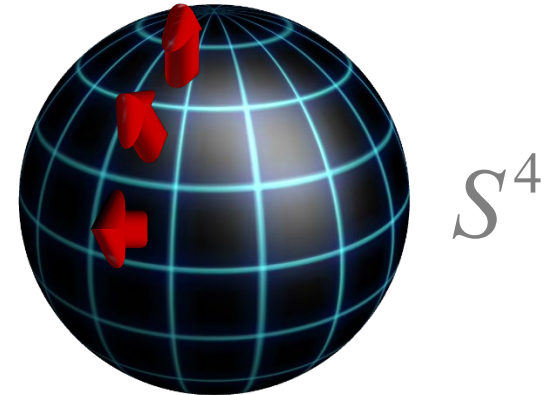


Phys. Rev. Lett. 115, 195303 (2015)

4D quantum Hall effect



Phys. Rev. Lett. 115, 195303 (2015)



J. Fröhlich and B. Pedrini, *Mathematical Physics* (2000)
 S.-C. Zhang and J. Hu, *Science* 294, 823 (2001)

quantized transverse non-linear response

$$I_\alpha = C_2 \frac{e^2}{h} \varepsilon_{\alpha\beta\gamma\delta} B_\beta E_\gamma E_\delta$$

2nd Chern number

Collaborators

Open Kondo box



W. Wegscheider



K. Ensslin



M. S. Ferguson



G. Blatter

Atomic topological pump



Monika Aidelsburger
(LMU)



Michael Lohse



Christian Schweizer



Immanuel Bloch
(LMU)

Ioannis Petrides
(Harvard)



Jan Kosata

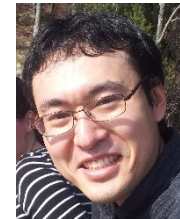


Jose L. Lado
(Aalto)

4D Topology



Hannah Price
(Birmingham)



Tomoki Ozawa
(Tohoku)



Nathan Goldman
(ULB)



Iacopo Carusotto
(Trento)



The quest continues



Thank you!