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ETH

Reduced Limit on the Permanent Electric Dipole Moment of the Neutron

UNIVERSITÄT MAINZ



PSI LTP Colloquium 2020/10/08 P. Schmidt-Wellenburg

PB

PHYSICAL REVIEW LETTERS 124, 081803 (2020)

University of Sussex

Editors' Suggestion Featured in Physics

Measurement of the Permanent Electric Dipole Moment of the Neutron

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A Publication by and for the ORNL Employees of Carbide and Carbon Chemicals Division, Union Carbide and Carbon Corporation

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HARVARD UNIVERSITY SPONSORS PROGRAM HERE — James H. Smith, Harvard University graduate student in physics, is shown as he adjusts a neutron beam apparatus at the south face of the Oak Ridge Pile. Using the Pile as a source of neutrons, Mr. Smith is engaged in a project jointly sponsored by Harvard University and Oak Ridge National Laboratory for the purpose of determining if neutrons have permanent electric dipole moments.

OAK RIDGE, TENNESSEE

Harvard University Conducts Important Research at ORNL

The growing importance of Oak Ridge National Laboratory as a research center is manifested particularly in its assistance to universities and technical schools on various projects in which nuclear research is involved. An example of such relationship is its present collaboration with Harvard University in an investigation to determine if neutrons have permanent electric dipole moments.

The work of the project is under the direction of Professors E. M. Purcell and Norman F. Ramsey of the Harvard University Physics. Department and is being conducted on the Laboratory area by James H. Smith, a



Friday, September 29, 1950

A brief history of EDM searches





58









P. Schmidt-Wellenburg

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CP violation & EDM





Insufficient CP-violation to explain origin of matter

The **CP**-violating phase of the CKM matrix cannot explain the observed baryon asymmetry of the Universe.

Additional sources of CP-violation beyond the standard model are needed.

Sakharov criteria* 1. Baryon number violation

- 2. C and CP violation
 - 3. Thermal nonequilibrium

*[A. D. Sakharov, JETP 5 (1967), 32]



PAUL SCHERRER INSTITUT Testing electro-weak baryogenesis





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neutron EDM

 $d_{n} = 3 \times 10^{-27} \text{ e cm}$

 $d_{e} = 10^{-27} e cm$

 $d_n = 3x10^{-28} e cm$

 $d_{n}=10^{-28} e cm$

300

250







 $\sin(\phi_{M_1})$

Complementarity of EDM searches





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- Several measurement of the electron EDM have different sensitivities to different CPV terms
- Adding the mercury EDM which by itself is hardly sensitive to the eEDM constraints the C_s -eEDM correlation.









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 $d = \frac{h\Delta f}{4E}$

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Ramsey's technique to measure f





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Coupling of the spin to an electric field









The hardware:

A historical interlude



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The history of the Sussex tin can





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The history of the Sussex tin can

















 Sensitivity for many cycles ideal case:

$$\sigma(d_{\rm n}) = \frac{\hbar}{2\alpha TE\sqrt{NM}}$$

Only if magnetic field is stable enough.
 (Good fit with orange, bad fit with purple)















- Options with field changes:
- Change E-field with adequate period (e.g. every 10 cycles) (loose time due to E ramps)
- Use a stack of two neutron precession chambers
- Use a comagnetometer



Sussex's co-magnetometer

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The nEDM spectrometer





Mercury comagnetometer



998) 38 129 Green et al., **NIMA** 404 (1998 Ban et al., **NIMA** 896 (2018) y. G

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Pendlebu

Pignol



and the oscillation ω_r is a result of rapidly changing trajectories, e.g. $\omega_r = v_r/2R$

 $\Delta \omega = \frac{(\gamma_n B_\perp)^2}{2(\nu_n B_0 - \omega_r)}$

 $B_{\perp} = \frac{\partial B_z}{\partial z} \frac{r}{2} + \frac{v_r E}{c^2}$

Motional magnetic field from $B_{\rm m} = -\frac{\nu \times E}{c^2}$

In non-uniform B-field and E-field:

with

resonance frequency by

Naively no contribution as $\bar{v} = 0$ for UCN?

Rabi: Spin rotation due to oscillating horizontal field.

This leads to a shift (Ramsey, Bloch, Siegert) of the

$v \times E$ the dominant systematic







 $\frac{v \times E}{c^2}$ Motional magnetic field from $B_{\rm m}$

In non-uniform B-field and E-field:

$$B_{\perp}^{2} = \left(\frac{\partial B_{z}}{\partial z}\frac{r}{2}\right)^{2} + r\frac{\partial B_{z}}{\partial z}\frac{v_{r}E}{c^{2}} + \left(\frac{v_{r}E}{c^{2}}\right)^{2}$$

The term linear in E will lead to a electric field induced shift of precession frequency, an EDM like signal.

$$\Delta \omega_{\rm f} = r \frac{\partial B_z}{\partial z} \frac{v_r E}{2c^2 (\gamma_{\rm n} B_0 - \omega_r)}$$

Different for neutrons (adiabatic), and mercury (ballistic/non-adiabatic)





(201 93 PLB Guillaume Pignol **Pignol and** Ū

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Measure EDM vs G_{1.0}



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Cesium magnetometer array for field gradients







Use polynomial decomposition to calculate non-uniform field

$$\vec{B}(\vec{r}) = \sum_{l,m} G_{l,m} \begin{pmatrix} \Pi_{x,l,m}(\vec{r}) \\ \Pi_{y,l,m}(\vec{r}) \\ \Pi_{z,l,m}(\vec{r}) \end{pmatrix}$$



 $\sigma(G_{1.0}) \approx 8 \,\mathrm{pT/cm}$

Not sufficient to correct for systematic

• Center of mass offset
• Center of mass offset
• Non-adiabaticity

$$R_{\pm} = \frac{f_{n}}{f_{Hg}} = \left| \frac{\gamma_{n}}{\gamma_{Hg}} \right| (1 \pm \delta_{EDM} \pm \delta_{EDM}^{false} + \delta_{Q} + \delta_{G} + \delta_{T} + \delta_{E} + \delta_{LS} + \delta_{I} + \delta_{P} + \delta_{AC})$$

$$\frac{\gamma_{Hg}}{2\pi} \approx 8 \text{ Hz/}\mu T$$

$$\frac{199 \text{ Hg}}{\overline{\gamma_{Hg}}} = 160 \text{ m/s vs. } \overline{\nu_{UCN}} \approx 3 \text{ m/s}$$

$$R \cdot \left| \frac{\gamma_{n}}{\gamma_{Hg}} \right| - 1 = \delta_{G} = \pm \frac{\langle z \rangle G_{1,0}}{B_{0}}$$

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• Center of mass offset
• Center of mass offset
• Non-adiabaticity

$$R_{\pm} = \frac{f_{n}}{f_{Hg}} = \left| \frac{\gamma_{n}}{\gamma_{Hg}} \right| (1 \pm \delta_{EDM} \pm \delta_{EDM}^{false} + \delta_{Q} + \delta_{G} + \delta_{T}) + \delta_{E} + \delta_{LS} + \delta_{I} + \delta_{P} + \delta_{AC})$$

$$\frac{\gamma_{Hg}}{2\pi} \approx 8 \text{ Hz/}\mu T$$

$$\boxed{P_{Hg}} \approx 160 \text{ m/s vs. } \overline{\nu_{UCN}} \approx 3 \text{ m/s}$$

$$R \cdot \left| \frac{\gamma_{n}}{\gamma_{Hg}} \right| - 1 = \delta_{G} + \delta_{T} = \pm \frac{(z)G_{1,0}}{B_{0}} + \frac{(B_{T}^{2})}{2B_{0}^{2}}$$
Needs to be known for each measurement

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Maximize field uniformity



P. Schmidt-Wellenbu

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- Use known sensitivity of each CsM to changes of any of 30 trim coils
- Use field information from offline field maps for $\langle B_{\rm T}^2 \rangle$

Initial polarization (prior $\pi/2$ flip) $\alpha_0 = 0.86$ Best polarization after 180 s free precession $\alpha_{180} = 0.81$

Average:

 $\overline{\alpha_{180}} = 0.76$

$$T_{2} = -180s / \ln\left(\frac{a_{180}}{\alpha_{0}}\right) = 3000s$$
$$\overline{T_{2}} = -180s / \ln\left(\frac{\overline{a_{180}}}{\alpha_{0}}\right) = 1315s$$













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Shift the central value by adding an unknown offset EDM of -1.5 to 1.5E-25 ecm to the data

Blinding

$$\delta N_{\uparrow,\downarrow;i} = \mp \bar{N} \frac{\pi \alpha}{\Delta \nu} \frac{d \cdot E}{h} \sin \phi_i$$
with $\phi_i = \frac{(\nu_i - \nu_0)}{\Delta \nu} \pi$

- Keep un-blinded data in a safe place (encrypted)
- Two blinding levels
 - Primary blinding same for Ο both analysis groups
 - Secondary blinding layer different for 0 both groups







Path to a new result (PSI)

Previous result (ILL), J.M. Pendlebury et al, Phys. Rev. D 92 092003 (2015)

 $d_n = (-0.2 \pm 1.5_{\text{stat}} \pm 1.0_{\text{syst}}) \times 10^{-26} \text{ ecm}$




S



- Schmidt-Wellenburg
- Each set has one fixed gradient (typically 48h long)
- Each set is subdivided into subsets with at least two E-field reversals (ABBA) with
 A = ±E and B inverse
- Length of typical subset approximately 112 cycles
- SFI at entrance was flipped every 112 cycles

| | 0AA0BB | 0A | A0BB | 0A | A0BB | 0A | |
|----|--------|----|------|----|------|----|-----|
| | 0AA0BB | 0A | A0BB | 0A | A0BB | 0A | A0B |
| F1 | 0 | | 1 | | 0 | | 1 |

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- æ
- lenburg



- A total of 8 fit parameters Ο
- Parameter errors are small Ο due to high number of dof.









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Gradient drift correction



For each subset a relative gradient Δg was calculated:

- Exclude sensors at high voltage
- Use 9 ground CsM and HgM
- Subtract mean value of each sensor for entire subset
- Polynomial expansion up to second order
- Use G_{10} and error for correction







Remaining drifts in R required to employ an R vs (t, E) fit: Minimize $(R - Ax)^{-1}C^{-1}(R - Ax)$

with

$$Ax = \begin{bmatrix} 1 & t_1 - \langle t \rangle & E_1 \\ 1 & t_2 - \langle t \rangle & E_2 \\ \vdots & \vdots & \vdots \\ 1 & t_n - \langle t \rangle & E_3 \end{bmatrix} \begin{pmatrix} R_{\text{sub}} \\ dR/dt \\ a \end{pmatrix}.$$

From a we deduce the EDM for each subset:





Time since start of subsequence (h)

gui







Previous result (ILL), J.M. Pendlebury et al, Phys. Rev. D 92 092003 (2015)

 $d_n = (-0.2 \pm 1.5_{\text{stat}} \pm 1.0_{\text{syst}}) \times 10^{-26} \text{ ecm}$





Hg EDM

effects

False

)ther





Table I: Summary of systematic effects in $10^{-28} e$ cm. The first three effects are treated within the crossing-point fit and are included in d_{\times} . The additional effects below the line are considered separately.

| Effect | shift error | |
|---|-------------|-------|
| Error on $\langle z \rangle$ | | |
| Higher order gradients \hat{G} | | Field |
| Transverse field correction $\langle B_{\rm T}^2 \rangle$ | | |
| Hg EDM[8] | | |
| Local dipole fields | | |
| $v \times E$ UCN net motion | | |
| Quadratic $v \times E$ | | |
| Uncompensated G drift | | |
| Mercury light shift | | |
| Inc. scattering ¹⁹⁹ Hg | | |
| TOTAL | | |

mapping

Schmidt-Wellenburg









Crossing point analysis

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The crossing point analysis takes care of a large part of the motional false EDM:

$$d_{n \leftarrow Hg}^{\text{false}} = \frac{\hbar \gamma_n \gamma_{Hg}}{32c^2} D^2 \left[G_g + G_{30} \left(\frac{D^2}{16} + \frac{H^2}{10} \right) + G_{50} \left(\frac{H^4}{28} - \frac{D^2 H^2}{96} - \frac{5D^4}{256} \right) \right]$$

Corrected by
crossing point fit

Corrected set for set using map analysis



False Hg EDM

effects

)ther







Table I: Summary of systematic effects in $10^{-28} e$ cm. The first three effects are treated within the crossing-point fit and are included in d_{\times} . The additional effects below the line are considered separately.

| | Effect | shift | error | |
|---|---|------------------------|-------|----------------------------------|
| | Error on $\langle z \rangle$ | - | 7 | |
| | Higher order gradients \hat{G} | 69 | 10 | Field monning |
| | Transverse field correction $\langle B_{\rm T}^2 \rangle$ | 0 | 5 | Field mapping |
| | Hg EDM[8] | -0.1 | 0.1 | |
| | Local dipole fields | - | 4 | |
| | $v \times E$ UCN net motion | - | 2 | |
| | Quadratic $v \times E$ | - | 0.1 | |
| | Uncompensated G drift | - | 7.5 | |
| | Mercury light shift | - | 0.4 | |
| I | Inc. scattering ¹⁹⁹ Hg | - | 7 | \leftarrow was not anticipated |
| | TOTAL | 69 | 18 | therefore poorly controlled |

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Pseudo magnetic field from incoherent scattering length b_i of mercury







 $\delta\eta = \eta(+E) - \eta(-E)$

- I = 1/2 nuclear angular momentum
- $b_i = \pm 15.5 \text{ fm}$
- nP (¹⁹⁹Hg × polarization) extracted from data cycle by cycle

$$d_{\rm n}^{\rm false} = \hbar \frac{\gamma_{\rm n}}{4E} B^* \cdot \delta \eta$$

 $< 7 \times 10^{-28} e cm$







Previous result (ILL), J.M. Pendlebury et al, Phys. Rev. D 92 092003 (2015)

 $d_n = (-0.2 \pm 1.5_{\text{stat}} \pm 1.0_{\text{syst}}) \times 10^{-26} \text{ ecm}$

 $d_n = \left(\begin{bmatrix} 2 \\ 3 \end{bmatrix} \pm 1.1_{\text{stat}} \pm 0.2_{\text{syst}} \right) \times 10^{-26} e \text{cm}$



d_{\times} (10⁻²⁶ ecm) THE WEST THE EAST

DOUBLE BLIND

SINGLE BLIND

UNBLIND

15.4 ± 1.1



3.8 ± 1.1

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Previous result (ILL), J.M. Pendlebury et al, Phys. Rev. D 92 092003 (2015)

$$d_n = (-0.2 \pm 1.5_{\text{stat}} \pm 1.0_{\text{syst}}) \times 10^{-26} \text{ ecm}$$

$$d_n = (0.0 \pm 1.1_{\text{stat}} \pm 0.2_{\text{syst}}) \times 10^{-26} \text{ ecm}$$

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The new limit







Global limit on theta



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Different EDM searches have different sensitivities to the θ -term and other underlying effective parameters. In general one can describe any EDM as $d_i = \sum \alpha_{ii} C_i$

where α_{ii} is the sensitivity to the EFT parameter C_i for a specific EDM d_i .

Unconstraint fit to all EDM limits using all nucleon parameters $(C_T, g_{\pi}^0, g_{\pi}^1, d_n^{SR})$:

 $-9 \times 10^{-8} < \theta < 0.2 \times 10^{-8}$

```
(Global d_e and C_s subtracted.)
```



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Backup





The crossing point analysis takes care of a large part of the motional false EDM:

$$d_{n \leftarrow Hg}^{\text{false}} = \frac{\hbar \gamma_n \gamma_{Hg}}{32c^2} D^2 \left[G_g + G_{30} \left(\frac{D^2}{16} + \frac{H^2}{10} \right) + G_{50} \left(\frac{H^4}{28} - \frac{D^2 H^2}{96} - \frac{5D^4}{256} \right) \right]$$

Corrected by
crossing point fit

Corrected set for set using map analysis







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Frequency for each cycle







Data point below cosine: $A_i < (A_{SF2} - \alpha)$



ideal case:

• Requires:

Sensitivity versus Stability



- g M

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 $\sigma_{\rm stat}(B) = \frac{1}{\gamma_{\rm n} \alpha T \sqrt{NM}}$

 Sensitivity for many cycles Allan deviation:

$$\sigma_{AD}(M) = \sqrt{\frac{\left\langle \left(f_i(M) - f_{i-1}(M)\right)^2 \right\rangle}{2}}$$



Choose *M* such that:

 $\sigma_{\text{stat}}(M) \geq \sigma_{AD}(M)$



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 Many cycles sensitivity ideally: $\sigma_{\rm stat}(B) = \frac{-}{\gamma_{\rm n} \alpha T \sqrt{NM}}$ • Require: $\sigma_{\text{stat}} \geq \overline{\Delta B}$ $\frac{\langle f_n \rangle}{\langle f_n \rangle^2} = \frac{\langle (f_n^A - f_n^{A-1})^2 \rangle}{\langle f_n \rangle^2} M = 4$

Allan deviation:

$$\sigma_{AD}(M) = \sqrt{\frac{\left\langle \left(f_i(M) - f_{i-1}(M)\right)^2 \right\rangle}{2}}$$





The full covariant matrix C



$$A_i = A_{\rm av} - \alpha \cos\left(\frac{\omega_{\rm rf} - \omega_{\rm cor}}{\Delta \nu} + \phi\right) \rightarrow f = \frac{\Delta \nu}{\pi} \left[\arccos\left(\frac{(A_{\rm av} - A_i)}{\alpha}\right) + \phi \right]$$

$$C = C_{\alpha} + C_{A_i} + C_{A_{av}} + C_{\phi}$$

 $C_{A_{\mathrm{av}},ij} = \frac{\mathrm{d}f}{\mathrm{d}A_{\mathrm{av},i}} \cdot \frac{\mathrm{d}f}{\mathrm{d}A_{\mathrm{av},j}} \cdot \delta A_{\mathrm{av},i} \,\delta A_{\mathrm{av},j}$

Remember there are four different A_{av}

$$=\frac{\Delta v^{2} \delta A_{\text{av},i} \, \delta A_{\text{av},j}}{\pi^{2}} \left(\alpha^{2} - \left(A_{\text{av},i} - A_{i}\right)^{2}\right)^{-1/2} \left(\alpha^{2} - \left(A_{\text{av},j} - A_{j}\right)^{2}\right)^{-1/2}$$

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The full covariant matrix C



$$A_i = A_{\rm av} - \alpha \cos\left(\frac{\omega_{\rm rf} - \omega_{\rm cor}}{\Delta \nu} + \phi\right) \rightarrow f = \frac{\Delta \nu}{\pi} \left[\arccos\left(\frac{(A_{\rm av} - A_i)}{\alpha}\right) + \phi \right]$$

$$C = C_{\alpha} + C_{A_i} + C_{A_{av}} + C_{\phi}$$

$$C_{\alpha,ij} = \frac{\mathrm{d}f}{\mathrm{d}\alpha_i} \cdot \frac{\mathrm{d}f}{\mathrm{d}\alpha_j} \cdot \delta\alpha^2 = \frac{\Delta\nu^2 \delta\alpha^2}{\alpha^2 \pi^2} \frac{\left(A_{\mathrm{av},i} - A_i\right)}{\sqrt{\alpha^2 - \left(A_{\mathrm{av},i} - A_i\right)^2}} \frac{\left(A_{\mathrm{av},j} - A_j\right)}{\sqrt{\alpha^2 - \left(A_{\mathrm{av},j} - A_j\right)^2}}$$

$$C_{\phi,ij} = \frac{\mathrm{d}f}{\mathrm{d}\phi_i} \cdot \frac{\mathrm{d}f}{\mathrm{d}\phi_j} \cdot \delta\phi\delta\phi = \frac{\Delta\nu^2\delta\phi^2}{\alpha^2\pi^2}$$

Remember there are four different A_{av}



- Calculate R
- Divide covariance matrix by matrix f'_{Hg,ij}
 (element for element)
- Add diagonal matrix with statistical error for each R value

 $R = \frac{f_{\rm n} \mp \gamma_n / 2\pi \langle z \rangle g_z}{f_{\rm Hg}}$

$$f_{\mathrm{Hg},ij} = f_{\mathrm{Hg},i} \cdot f_{\mathrm{Hg},j}$$

$$\sigma_R^2 = \frac{\sigma_{f_{\rm Hg}}^2}{f_{\rm Hg}^2} + \left(\frac{\gamma_n/2\pi\langle z\rangle\,\delta g_z}{f_{\rm Hg}}\right)^2 + \left(\frac{\sigma_{\rm Hg}\cdot(f_{\rm hg}\mp\gamma_n/2\pi\langle z\rangle\,\delta g_z)}{f_{\rm Hg}^2}\right)^2$$



R value and error on R

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Main features of the new instrument





Inspired by Gatchina double-chamber setup I.Altarev et al. JETP Lett.44(1986)460 and based on years of experience with our own operating experiment:

- 2 neutron precession chambers
- Hg co-magnetometer in both chambers with laser read out
- Baseline scenario: UCN chamber with materials and coatings as present chamber, but larger diameter of storage volume - upgrades in development

- Surrounded by calibrated Cs arrays on ground potential ($\sim 100~{\rm sensors})$

- large NiMo (58NiMo) coated UCN guides



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Analysis: Frequency ratio $R = f_n/f_{Hg}$



double chamber - linear $\partial B/\partial z$ is almost perfectly compensated but due to different h_t and h_b gradient fluctuations still cause an error on a lower level though

$$R^{\mathrm{T}} - R^{\mathrm{B}} = \frac{\gamma_{\mathrm{n}}}{\gamma_{\mathrm{Hg}}} \left(2\delta_{\mathrm{EDM}} + (\langle z \rangle_{\mathrm{T}} - \langle z \rangle_{\mathrm{B}}) \frac{g}{B_{0}} + \cdots \right)$$

Analysis: based on $(R^{T} - R^{B})$ as function of dB/dz extrapolate to 0



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Magnetically Shielded Room



? Schmidt-Wellenburg

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setup features:

- (2 + 4) layers mu-metal
- Al eddy current shield
- 78 openings for experiment use
- largest openings
 ID=220mm
- for 2 UCN guides
- for 2 main pumping ports

expected performance: - quasi-static shielding factor guaranteed >70'000 (expected >100'000) - central B-field < 0.5nT

- central gradient < 0.3 nT/m




Excellent B-field uniformity



Magnetic-field generation

- Optimized main magnetic field coil
- 64 correction coils

Magnetic-field measurement

- Order 100 CsM sensors
- Optimal placement



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Today's status of n2EDM



Status of setup:

- MSR installed and commissioning has started
- Installation of coil system, vacuum tank and precession chambers next
- Area and environmental setup ongoing



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